## FLUX PINNING IN HIGH TEMPERATURE SUPERCONDUCTORS INVESTIGATED BY MAGNETIC RELAXATION MEASUREMENTS

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Different methods for the analyses of measurements of the time dependence of the magnetic moment in high  $T_c$  superconductors are discussed. Examples are given for Bi2223-tapes, powder-melt-processed (PMP) YBCO with different oxygen content and melt-textured YBCO with an enhanced fishtail effect. Bi2223 tapes show 2D flux creep behaviour. Whereas in fully oxygenated YBCO 3D behaviour is obtained, a tendency towards 2D is found if the oxygen content is reduced or a pronounced fishtail is present.

In the Shubnikov phase of a superconductor flux lines arrange themselves in a way, such that the Lorentz force, which drives the flux lines into the material is on every point in equilibrium with the pinning force. This equilibrium defines the critical state [1]. As Anderson [2] pointed out, a possibility exists for flux movement away from this critical state, because of thermal activation at nonzero temperatures. According to Andersons theory of flux creep 'flux bundles' jump over pinning barriers with a rate according to an Arrhenius law  $\nu = \nu_0 \exp(-U/kT)$ , where  $\nu_0$  is an attempt frequency and U the effective activation energy, which increases monotonically with time, leading to a logarithmic time dependence of M(t). In its simplest form [3] U is given by  $U = U_0 - |F|VX$  where F is the driving force, V the flux bundle volume and X the hopping distance or pinning length. For  $U \gg kT$  the deviation of the system from the critical state is small. Then |F| is equal to the elementary pinning force  $F_p = J_c B$  and the effective pinning barrier is given by  $U_0 = J_c BVX$ . Whereas from measurements of the critical current density  $J_c$  only the relation  $U_0/VX$  can be deduced, the measurements of the time decay of the magnetic moment allows in principle to determine  $U_0$  and VX independently.

By the flux diffusion equation [4]  $\partial B/\partial t = \nabla [BX\nu_0 \exp(-U/kT)]$  (B is the local field), the logarithmic time dependence of the magnetic moment follows under the assumption  $U\gg kT$ . This condition is fulfilled for classical superconductors, but in high temperature superconductors U is normally much lower, because the coherence length  $\xi$  is much smaller and kT is very large for temperatures near  $T_c$ . Nevertheless numerical calculations of the flux diffusion equation [5] show that 90% of the relaxations in high  $T_c$  superconductors are expected to be also logarithmic. The simplification, when

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assuming only one barrier height can be overcome by taking into account a distribution of activation energies [6]. Also the ansatz of a linear U(J)-relation is very crude, because it implies a V-notch like shaped pinning potential. For physically more realistic potential shapes, nonlinear U(J)-relations are always the consequence. It was shown [6], that for a wide variety of different shapes  $U \sim U_p (1-J/J_{max})^n$  with 3/2 < n < 2 is a good approximation.  $J_{max}$  is the maximum current density which pinning potential can sustain in the absence of thermal activation.  $U_p$  is the true pinning well height. The Anderson-Kim relation is described by the tangent on the real U(J)-curve at that current density, which corresponds to the momentary measuring conditions. Therefore large differences between the linearly extrapolated  $U_0$ -value and the real pinning potential barrier height  $U_p$  may appear.

all other temperatures on a smooth curve. determined from the constants, which are necessary to bring the relaxation curves for where Tirr is the irreversibility temperature. A third possibility is to use a value for with  $t = T/T_c$ . Sometimes better results have been obtained by using  $t = T/T_{irr}$  [10], damentally related to pinning. A Ginzburg-Landau treatment leads to  $g(T) \sim (1-t^2)$ should be governed by the temperature dependence of those parameters, which are funkham [9] has proposed, that the temperature dependence of the pinning well height temperatures a change in the pinning well height U has to be taken into account. Tin-The smoothness can be reached only in the low temperature region, because at higher results do not depend very much on C, because it is only a logarithmic correction term. dent, follows from the condition, that all points have to lie on a smooth curve. The of the sample. The appropriate C value, which is assumed to be temperature indepenmula [1]. The parameter C follows from  $C = \ln(H_a \nu_0 X/2\pi d)$ , where d is the thickness by plotting  $-T \ln |dM(t)/dt| + CT$  against  $M_{irr}$ , which is related to  $J_c$  via Beans for-C, obtained only from the fit to the low temperature regime (T < 15 K). g(T) is then As pointed out by Maley et al [8], the shape of the U(J)-relation can be determined

A logarithmic U(J)-dependence was proposed from the analysis of resistivity measurements for a variety of different samples [11]. A more general equation was suggested by Feigel'man et al [12] on the basis of the collective pinning theory, where the pinning on randomly distributed weak pinning centres is discussed by taking into account the elasticity of the flux line lattice. Because of the small coherence length  $(\xi)$ , tiny defects (e.g. oxygen vacancies, dislocations) are effective pinning centres. This theory predicts for  $J \ll J_c$  an inverse power law  $U = U_i(J/J_c)^{-\mu}$ , where  $U_i$  is the activation energy for  $J = J_c$  and the exponent  $\mu$  is dependent on the dimensionality and the particular flux creep regime. An interpolation formula for the whole J region is given by  $U = U_i[(J_c/J)^{\mu} - 1]$ , where for  $\mu = -1$  the Anderson and for  $\mu = 0$  the Zeldov equation is obtained. In the case of 3D pinning  $\mu = 1/7, 3/2$  and 7/9 is expected [12] for pinning of single vortices, small flux bundles (sfb) and large flux bundles (lfb), respectively. If  $\xi$  is smaller than the distance of the superconducting layers, flux decouples into so called pancakes and 2D flux creep takes place. In that case  $\mu = 9/8$  (svc) and 1/2 is proposed [13,14] for single vortex (svc) and collective vortex creep (cvc).

There are two possibilities to analyse the U(J)-curves in terms of the collective pinning theory: i) to fit them by the interpolation formula ii) to do it graphically by

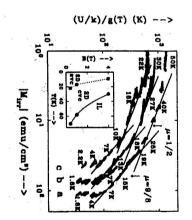
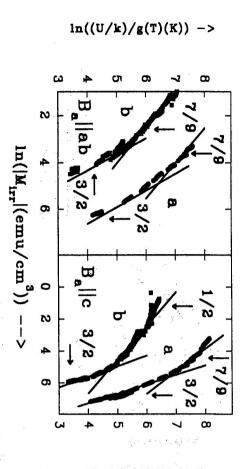


Fig.1 U(J)-relation for a Bi2223-tape measured at 1 T (a), 3 T (b) and 5 T (c), ( $C = 15, g(T) = 1 - (T/T_c)^2, T_c = 106 \text{ K, IL}$  irreversibility line).

plotting  $\ln(U)$  vs  $\ln(|M_{frr}|)$ . In the first case the full J region can be covered, but in the fit  $\mu$  is constrained to be independent of temperature. Therefore a fit may lead to wrong  $\mu$  values, when  $\mu$  depends on the current density. This can be checked, if the fit is performed for different temperature intervals. In the graphic representation  $\ln(U)$  vs  $\ln(|M_{frr}|)$   $\mu$  appears as the slope on the curve, according to the invers power law. This method has the disadvantage, that it is only applicable for current densities  $J \ll J_c$ . One can assume that this condition is fulfilled in most of the temperature range, because due to the small sweep rate used for the measuring field the critical state is never reached. The best proof for this assumption is fitting the low temperature regime by the interpolation formula and comparing the obtained exponent  $\mu$  with the slope obtained from the graphic analysis. If they are equal, the condition  $J \ll J_c$  should be fulfilled.

c-direction. In that case theory predicts  $\mu = 9/8$  if the pancakes are moving indepening effects. The change from single vortex creep to collective vortex creep is shifted analysis in terms of activation energy distributions where the relaxation time  $\tau$  is reulus  $c_{66} = (B_c^2/4\mu_0)b(1-b^2)$ ,  $b = B/B_{c2}$  and  $\xi_{ab}$  the coherence length in ab-direction) reached, if the transverse coherence length  $R_c \sim (c_{66}\xi_{ab}/J_cB)^{1/2}$  (with the shear moddently, and  $\mu = 1/2$  if they creep collectively. The border between the two regimes is large distance between the CuO2 sheets, which is larger then the coherence length in a double logarithmic representation for three different fields applied perpendicular to  $T_c$  superconductors are given. In Fig.1 the U(J)-curves for a Bi2223-tape are shown in dence of the magnetic moment performed in a VSM on three different textured high lact that the condition  $J \ll J_c$  is not fulfilled, or by the influence of quantum tunnellated to V by  $\tau = 2\mu_0 kT/(2\pi\nu_0 V B_a^2)$ . Both regimes are observed in the measurements the activation volume V should be smaller than or equal to the one of a single pancake becomes larger than the vortex lattice spacing  $a_0 \sim (\phi_0/B_a)^{1/2}$ . For single vortex creep the tape surface. For Bi-superconductors a 2D behaviour is expected, because of the (Fig.1). The extreme large  $\mu$ -value at low temperatures may either be caused by the  $V_{pc} \sim a_0^2 s$  (s is the distance between the CuO<sub>2</sub> planes). V can be obtained from an In the following, examples for such analysis of the measurements of the time depen-



62 K (b) measured at 3 T; C = 15,  $g(T) = 1 - (T/T_c)^2$ . Fig. 2 U(J)-relation for powder-melt-processed (PMP) YBCO samples with  $T_c = 92 \text{ K}$  (a) and

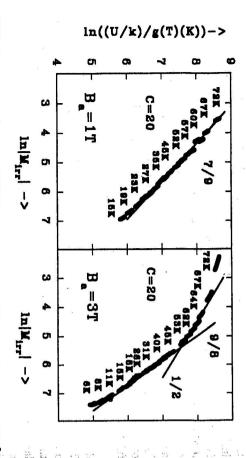


Fig.3 U(J)-relation for melt-textured YBCO, determined for  $B_a \parallel c$  with  $g(T) = 1 - (T/T_c)^2$ .

given equations.  $R_c$  increases with field, because of the decrease of  $J_c$  with increasing to lower temperatures for higher fields (Inset Fig.1). This is expected from the above

length compared to the Bi-samples. The system changes from small flux bundle creep 92 K 3D behaviour is obtained, as expected for YBCO, because of the larger coherence powder-melt-processed (PMP) YBCO samples. As seen in Fig.2 for a sample with  $T_c =$ As a second example we discuss results obtained from measurements of textured

> 3D) at low temperatures to collective pinning in 2D at lower current densities (Fig.2). 92 K sample (only  $J_c$  is reduced), but for  $B_a || c \mu$  changes from 3/2 (sfb pinning in is shown in Fig.2 for a sample with  $T_c=62$  K. For  $B_a\|(a,b)$   $\mu$  is the same as for the when the oxygen content is reduced, pinning changes from 3D to 2D behaviour. This for these YBCO samples. Therefore a tendency towards 2D behaviour with decreasing oxygen content is found 3/2) to large flux bundle creep ( $\mu = 7/9$ ) with increasing temperature.

oxygen treatment. From flux creep measurements it is found, that at the field, where it can be concluded, that in this sample two different types of pinning centres exists single vortex creep to collective vortex creep in 2D with temperature appears. Therefore is dominated by the pinning centres which are responsible for the fishtail, a change from obtained in the temperature range 30 to  $70~\mathrm{K}$  (Fig.3a). At higher fields, where flux creep The sample exhibits a pronounced fishtail effect, which is strongly influenced by the behaviour of flux creep. in the usual 3D way, and the others, responsible for the fishtail effect, lead to a 2D The ones which can be detected in the field regime where no fishtail appears behave the sample behaves in the usual way: 3D pinning of large flux bundles ( $\mu = 7/9$ ) is the fishtail starts to develop, pinning behaviour changes drastically. Below this field In Fig.3 the results for a melt-textured YBCO sample with  $T_c=88~\mathrm{K}$  are shown.

grade of complexity exist, which all have various restrictions. But a combination of the in high temperature superconductors. For the analysis several methods of different an important method to get detailed information about the mechanisms of flux pinning different analyses lead to physically reasonable results. In conclusion, the investigation of the time dependence of the magnetic moment is

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