

# MOMENTS OF INERTIA AND COLLECTIVE GYROMAGNETIC RATIOS OF SOME OF THE DOUBLY EVEN NUCLEI IN THE RARE-EARTH REGION

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The moments of inertia and the gyromagnetic ratios of the ground states of some doubly even nuclei in the rare-earth region have been calculated using the cranking model formula. In the calculations the deformed shell-model asymptotic basis eigenfunctions with the inclusion of pair correlations have been used. Comparison with some of the available experimental data shows in general good agreement.

## I. INTRODUCTION

We consider the single-particle Hamiltonian given by Lamm [1] and also treated by Boisson and Piepenbring [2] as our starting point

$$\hat{H}_t = \hat{H}_0(\epsilon) + C l_t^z S + D(l_t^2 - \langle l_t^2 \rangle_{shell})$$

$$\hat{H}_0(\epsilon) = -\frac{\hbar^2}{2m} \Delta + \frac{1}{2} m [W_1^2(x^2 + y^2) + W_z^2 z^2], \quad (1)$$

where the subscript  $t$  stands for "transformed" or "stretched". Then the deformation parameter  $\epsilon$  is introduced which is defined by the following relations:

$$\begin{aligned} W_1 &= W_0(\epsilon)(1 + 1/3\epsilon) \\ W_z &= W_0(\epsilon)(1 - 2/3\epsilon). \end{aligned} \quad (2)$$

The condition of the conservation of the volume of the nucleus leads to

$$\begin{aligned} W_1^2 W_z &= \dot{W}_0^3 = \text{const.} \\ W_0(\epsilon) &= \dot{W}_0(1 - 1/3\epsilon^2 - 1/27\epsilon^3)^{-1/3}. \end{aligned} \quad (3)$$

We prefer to use the asymptotic basis of eigenvectors  $|MN_z\Lambda\Sigma\rangle$  since the expressions of the matrix elements become simpler. With this choice of the basis

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we write the single-particle eigenfunctions corresponding to  $\hat{H}_t$  given by equation (1) as follows:

$$|\Omega\rangle = \sum_{N_z\Lambda\Sigma} b_{N_z\Lambda\Sigma}^\Omega |NN_z\Lambda\Sigma\rangle. \quad (4)$$

In the single-particle state defined as  $|\Omega\rangle$ ,  $\Omega$  denotes the component of the total spin of the single-particle on the intrinsic  $z$ -axis (symmetry axis) as well as all other quantum numbers necessary for the specification of the state. On the other hand  $|\Omega\rangle$  has been normalized to unity. Furthermore, in order to be invariant under time reversal the system has to satisfy the condition

$$\hat{T}|\Omega\rangle = |-\Omega\rangle,$$

where  $\hat{T}$  is the time-reversal operator. Then one ends up with the time reversed state given by the following relation

$$|-\Omega\rangle = (-1)^{N+\sigma+\frac{1}{2}} \sum_{N_z\Lambda\Sigma} b_{N_z\Lambda\Sigma}^\Omega |NN_z - \Lambda - \Sigma\rangle. \quad (6)$$

The single-particle energies and the coefficients  $b_{N_z\Lambda\Sigma}^\Omega$  given in equations (4) and (6) can be determined by the diagonalization of the hamiltonian  $\hat{H}_t$  in the basis  $|NN_z\Lambda\Sigma\rangle$ .

The aim of this paper is to evaluate the gyromagnetic ratios and moments of inertia of the ground states of some doubly even nuclei in the rare-earth region using the cranking model formula.

## II. THE HAMILTONIAN OF THE NUCLEUS

In the second-quantization formalism the Hamiltonian of the nucleus is given by the relation

$$\hat{H} = \sum_{\nu>0} \epsilon_\nu \hat{N}_\nu - G \sum_{\nu,\nu'} a_\nu^\dagger a_{-\nu}^\dagger a_{-\nu} a_\nu, \quad (7)$$

where

$$\hat{N}_\nu = (a_\nu^\dagger a_\nu + a_{-\nu}^\dagger a_{-\nu}) \quad (8)$$

is defined to be the number operator such that

$$\hat{N} = \sum_\nu \hat{N}_\nu \quad (9)$$

is the total number operator. The other parameters entering into the Hamiltonian are the single-particle energies  $\epsilon_\nu$ , the pairing energy  $G$ , the creation and annihilation operators  $a^+$  and  $a$ , respectively.

The wave function which will be given in the following section is not an eigenfunction of the total number operator  $\hat{N}$ . In other words the number of particles is not conserved. On the other hand, the Hamiltonian  $\hat{H}'$  is introduced

$$H' = \hat{H} - \lambda \hat{N}, \quad (10)$$

which ensures the condition that the number of particles is conserved on the average.  $\lambda$  is a Lagrange multiplier which is also called the chemical potential.

The Bogolyubov—Valatin transformation [3] to quasi-particles is given to be

$$a_\nu = u_\nu a_\nu - v_\nu a_{-\nu}^+, \quad (11a)$$

$$\alpha_{-\nu} = u_\nu a_{-\nu} + v_\nu a_\nu^+, \quad (11b)$$

where  $u_\nu$  and  $v_\nu$  are real, free parameters such that  $u_\nu = 0, v_\nu = 1$  represents the occupied orbits, where as  $u_\nu = 1, v_\nu = 0$  represents the unoccupied orbits. Thus the normalization condition requires

$$u_\nu^2 + v_\nu^2 = 1. \quad (12)$$

By making use of this transformation the Hamiltonian  $\hat{H}'$  takes the form

$$\hat{H}' = U' + \hat{H}'_{11} + \hat{H}'_{20} + \hat{H}'_{22} + \hat{H}'_{31} + \hat{H}'_{40}, \quad (13)$$

where  $U'$  is a constant and the other terms may be expressed symbolically as  $\hat{H}_{ij}$ ,  $i$  and  $j$ , representing the numbers of the quasiparticle creation and annihilation operators, respectively. For example,  $\hat{H}_{31}$  contains the terms  $a^+ a^+ a^+ a$  and of them are given by Belyaev [4] and Eisenberg and Greiner [5].

### III. THE WAVE FUNCTION OF THE NUCLEUS

We consider the following wave function in order to minimize  $\hat{H}'$ :

$$\Psi_0 = \prod_\nu (u_\nu + v_\nu a_\nu^+ a_{-\nu}^+) |0\rangle. \quad (14)$$

As it has been mentioned above,  $\Psi_0$  is not an eigenfunction of the total number operator  $\hat{N}$  given by equation (9), i.e.  $N$  is not conserved. Then the Hamiltonian  $\hat{H}'$  is defined, which causes the condition that the average number of particles is conserved.

When the Bogolyubov—Valatin transformation is performed, one can show that

$$a_\nu |\Psi_0\rangle = 0, \quad (15)$$

which implies that the ground state  $\Psi_0$  of an even-even nucleus is the quasi-particles vacuum state.

The variational calculations for the solution of the ground state of the Hamiltonian  $\hat{H}'$  of equation (10), by the minimization of the expectation value of  $\hat{H}'$  with the eigenfunctions  $|\Psi_0\rangle$  provide the following relations:

$$U_\nu^2 = 1/2[1 + (\varepsilon_\nu - \lambda)/E_\nu] \quad (16a)$$

$$V_\nu^2 = 1/2[1 - (\varepsilon_\nu - \lambda)/E_\nu].$$

Where the definitions

$$E_\nu = \sqrt{(\varepsilon_\nu - \lambda)^2 + \Delta^2} \quad (17)$$

$$\Delta = G \sum_\nu U_\nu V_\nu \quad (18)$$

have been used. In these equations  $E_\nu$  is called the quasi-particle energy and  $\Delta$  the gap parameter.

### IV. MOMENT OF INERTIA AND COLLECTIVE GYROMAGNETIC RATIO

In order to obtain the expression for the moment of inertia in the quasiparticle formalism one first considers the well-known Inglis formula for the moment of inertia:

$$I = 2\hbar^2 \sum_{m \neq 0} |\langle m | \hat{j}_x | 0 \rangle|^2 / (\varepsilon_m - \varepsilon_0). \quad (19)$$

It is also borne in mind that the ground state of an even-even nucleus is the BCS ground state  $|\Psi_0\rangle$  given in equation (14). The angular momentum operator  $\hat{j}_x$  of equation (19) is a one-particle operator and thus it can be easily transformed to quasi-particle creation and annihilation operators using the inverse transformations of the equations (11a) and (11b). If the transformation is performed and the matrix elements  $\langle m | \hat{j}_x | \Psi_0 \rangle$  are computed, one can finally obtain the following expression

$$I = 2\hbar^2 \sum_{\nu, \nu'} |\langle \nu | \hat{j}_x | \nu' \rangle|^2 (u_\nu v_\nu - v_\nu u_\nu)^2 / (E_\nu + E_{\nu'}), \quad (20)$$

where  $u_\nu, v_\nu$  and  $E_\nu$  have already been defined. The explicit forms of the matrix elements of  $\hat{j}_x$  in the asymptotic basis are given in ref. [2].

The moment of inertia which is a measure of the mass transport of the collective rotational flow is an important quantity. Another quantity which is as important as the moment of inertia is the gyromagnetic ratio  $g_x$ . It measures the magnetic properties of the collective flow.

In the cranking model  $g_R$  is defined as the ratio between the average magnetic moment and the average angular momentum. The following expression is obtained when the collective gyromagnetic ratio is written by the inclusion of the pair-correlation interaction

$$g_R = I_p/I + (g_s^p - 1)W_p/I + g_s^n W_n/I, \quad (21)$$

where

$$(1/2\hbar^2)W_i = \sum_{v,v'} \langle v|J_x|v' \rangle \langle v|S_x|v' \rangle (u_v u_{v'} - v_v v_{v'})/(E_v + E_{v'}). \quad (22)$$

In the last two terms of equation (21)  $g_s^p$  and  $g_s^n$  represent the spin gyromagnetic ratios of proton and neutron, respectively.

## V. NUMERICAL CALCULATIONS

In the numerical calculations the parameters of the intrinsic Hamiltonian have been chosen such that for the Hamiltonian of equation (1) new parameters  $\mu$  and  $\chi$  are introduced in the terms of  $C$  and  $D$ :

$$\mu = \frac{2D}{C} \quad \chi = -C/2\hbar W_0, \quad (23)$$

where

$$\hbar W_0 = 41 \cdot A^{-\frac{1}{3}} \text{ MeV}. \quad (24)$$

The following  $\mu$  and  $\chi$  values are chosen for protons and neutrons, respectively:

$$\begin{aligned} \mu_p &= 0.60 & \chi_p &= 0.0637 \\ \mu_n &= 0.42 & \chi_n &= 0.0637. \end{aligned} \quad (25)$$

The gap parameters  $\Delta$  appearing in equations (17) and (18) are chosen in accordance with the work of Prior et al. [6]. First by means of  $\Delta_p$  and  $\Delta_n$ , then by  $p_p$  and  $p_n$  given by them, two sets of calculations are carried out. Later, taking  $\Delta_p = 12A^{\frac{-1}{2}}$  and  $\Delta_n = 11.2A^{\frac{-1}{2}}$ , which are the best average values extracted from the experimental curves, a third set of calculations has been carried out. The values of these parameters for different nuclei together with the calculated  $I$  and  $g_R$  values for each set of calculations are shown in tables 1–3.

All the calculations have been done by taking the values 0.20, 0.25, 0.30 for the deformation parameter  $\varepsilon$  defined by equations (2) and (3). In our calculations we have taken into account all states of the  $N = 4, 5, 6$  shells for protons and neutrons (64 levels for each).

Table 1a

Moment of inertia and collective gyromagnetic ratio of some of the doubly even nuclei for the gap parameters  $\Delta_p$  and  $\Delta_n$

$^{Z}X_N^A$	$\varepsilon$	$\Delta_p$ (keV)	$\Delta_n$ (keV)	$G_p$ XA	$G_n$ XA	$\frac{2}{\hbar^2} J_p$ (MeV) $^{-1}$	$\frac{2}{\hbar^2} J$ (MeV) $^{-1}$	$\frac{2}{\hbar^2} J_{\text{exp}}$ (MeV) $^{-1}$	$F = \frac{J}{J_{\text{exp}}}$	$\frac{2}{\hbar^2} W_p$ (MeV) $^{-1}$	$\frac{2}{\hbar^2} W_n$ (MeV) $^{-1}$	$g_R$
$^{62}\text{Sm}_{90}^{152}$	0.20	1167	1129	21.98	18.30	10.899	25.316	47.3	0.531	-0.606	-0.629	0.401
	0.25			23.07	18.32	14.144	36.318		0.768	-0.858	-1.011	0.388
	0.30			23.95	18.65	16.935	47.412		1.002	-0.986	-1.418	0.376
	0.20	1061	1068	21.44	18.01	12.614	30.478	73.2	0.416	-0.804	-0.824	0.396
	0.25			22.60	18.30	16.074	40.963		0.560	-0.987	-1.176	0.392
	0.30			23.52	18.64	18.877	50.769		0.696	-1.109	-1.511	0.385
	0.20	1108	1089	21.57	18.25	12.205	27.408	48.8	0.562	-0.795	-0.660	0.404
	0.25			22.60	18.27	15.113	38.421		0.787	-0.956	-1.066	0.385
	0.30			23.30	18.61	17.630	49.542		1.015	-1.090	-1.492	0.370
$^{64}\text{Gd}_{90}^{154}$	0.20	1013	1032	21.13	17.97	13.903	32.695	66.7	0.490	-0.912	-0.865	0.399
	0.25			22.20	18.27	16.911	42.965		0.644	-1.081	-1.233	0.388
	0.30			22.92	18.61	19.458	52.640		0.789	-1.218	-1.577	0.378
	0.20	962	953	20.97	17.62	14.943	38.051	75.0	0.507	-0.984	-1.099	0.385
	0.25			22.07	18.18	18.000	47.219		0.630	-1.157	-1.411	0.383
	0.30			22.80	18.46	20.550	55.892		0.745	-1.294	-1.711	0.379
	0.20	830	930	20.94	17.07	15.645	45.505	79.7	0.571	-1.032	-1.408	0.358
	0.25			22.05	17.89	18.731	54.127		0.679	-1.208	-1.728	0.366
	0.30			22.00	10.16	21.282	61.712		0.774	-1.345	-1.995	0.369

Table 1a continued

$zX_N^A$	$\varepsilon$	$\Delta_p$ (keV)	$\Delta_n$ (keV)	$G_p$ XA	$G_n$ XA	$\frac{2}{\hbar^2} J_p$ (MeV) $^{-1}$	$\frac{2}{\hbar^2} J$ (MeV) $^{-1}$	$\frac{2}{\hbar^2} J_{\text{exp}}$ (MeV) $^{-1}$	$F = \frac{J}{J_{\text{exp}}}$	$\frac{2}{\hbar^2} W_p$ (MeV) $^{-1}$	$\frac{2}{\hbar^2} W_n$ (MeV) $^{-1}$	$g_R$
$^{66}\text{Dy}_{94}^{160}$	0.20	937	913	20.93	17.54	15.653	40.217	68.5	0.587	-1.034	-1.169	0.383
	0.25			21.96	18.10	18.400	49.181		0.718	-1.164	-1.490	0.382
	0.30			22.42	18.38	20.235	57.203		0.835	-1.262	-1.797	0.373
$^{66}\text{Dy}_{96}^{162}$	0.20	891	803	20.82	17.06	16.774	47.962	74.0	0.648	-1.112	-1.474	0.361
	0.25			21.88	17.89	19.501	56.227		0.760	-1.242	-1.800	0.368
	0.30			22.34	18.15	21.225	62.989		0.851	-1.336	-2.072	0.366
$^{66}\text{Dy}_{98}^{164}$	0.20	858	637	20.79	16.25	17.648	61.539	80.8	0.762	-1.173	-1.977	0.322
	0.25			21.87	17.37	20.349	68.780		0.851	-1.302	-2.273	0.335
	0.30			22.33	17.68	21.901	71.384		0.883	-1.392	-2.326	0.343
$^{66}\text{Dy}_{100}^{166}$	0.20	828	680	20.77	16.54	18.501	56.867			-1.233	-1.418	0.321
	0.25			21.87	17.64	21.168	63.719			-1.361	-1.449	0.321
	0.30			22.34	10.26	22.705	67.264			-1.447	-1.464	0.322
$^{68}\text{Er}_{96}^{164}$	0.20	865	787	20.52	17.09	16.036	48.198	66.7	0.723	-1.062	-1.523	0.353
	0.25			21.39	17.93	18.672	56.373		0.845	-1.090	-1.853	0.368
	0.30			21.68	18.19	20.504	63.250		0.948	-1.139	-2.128	0.370
$^{68}\text{Er}_{98}^{166}$	0.20	827	622	20.43	16.30	16.917	62.077	74.1	0.838	-1.128	-2.040	0.315
	0.25			21.33	17.44	19.504	69.098		0.932	-1.145	-2.337	0.336
	0.30			21.62	17.75	21.238	71.606		0.966	-1.191	-2.383	0.348

Table 1a continued

$zX_N^A$	$\varepsilon$	$\Delta_p$ (keV)	$\Delta_h$ (keV)	$G_p$ XA	$G_h$ XA	$\frac{2}{\hbar^2} J_p$ (MeV) $^{-1}$	$\frac{2}{\hbar^2} J$ (MeV) $^{-1}$	$\frac{2}{\hbar^2} J_{\text{exp}}$ (MeV) $^{-1}$	$F = \frac{J}{J_{\text{exp}}}$	$\frac{2}{\hbar^2} W_p$ (MeV) $^{-1}$	$\frac{2}{\hbar^2} W_n$ (MeV) $^{-1}$	$g_R$
$^{68}\text{Er}_{100}^{168}$	0.20	800	685	20.42	16.73	17.581	55.609	75.0	0.741	-1.177	-1.402	0.316
	0.25			21.34	17.83	20.127	62.416		0.832	-1.187	-1.438	0.323
	0.30			21.63	18.46	21.786	66.168		0.882	-1.229	-1.454	0.328
$^{68}\text{Er}_{102}^{170}$	0.20	778	724	20.43	17.15	188.146	52.989	75.6	0.701	-1.219	-0.967	0.307
	0.25			21.37	18.29	20.656	60.711		0.803	-1.222	-0.883	0.304
	0.30			21.67	19.07	22.251	66.182		0.875	-1.262	-0.904	0.301
$^{70}\text{Yb}_{98}^{168}$	0.20	849	645	20.45	16.60	14.881	58.008			-0.928	-1.936	0.311
	0.25			20.94	17.73	18.209	66.031			-0.906	-2.235	0.342
	0.30			20.93	18.06	21.650	70.654			-0.880	-2.297	0.374
$^{70}\text{Yb}_{100}^{170}$	0.20	817	690	20.38	16.92	15.572	53.264	66.36	0.803	-0.980	-1.388	0.308
	0.25			20.89	18.03	18.923	60.950		0.918	-0.945	-1.426	0.329
	0.30			20.89	18.66	22.353	66.555		1.003	-0.910	-1.445	0.356

Table 1b

Moment of inertia and collective gyromagnetic ratio of some of the doubly even nuclei for the gap parameters  $\Delta_p$  and  $\Delta_h$ .

$Z X_N^A$	$\varepsilon$	$\Delta_p$ (keV)	$\Delta_h$ (keV)	$G_p$ XA	$G_h$ XA	$\frac{2}{\hbar^2} J_p$ (MeV) $^{-1}$	$\frac{2}{\hbar^2} J$ (MeV) $^{-1}$	$\frac{2}{\hbar^2} J_{\text{exp}}$ (MeV) $^{-1}$	$F = \frac{J}{J_{\text{exp}}}$	$\frac{2}{\hbar^2} W_p$ (MeV) $^{-1}$	$\frac{2}{\hbar^2} W_n$ (MeV) $^{-1}$	$g_R$
$^{70}\text{Yb}_{102}^{172}$	0.20	787	702	20.32	17.13	16.265	52.331	71.07	0.736	-1.032	-1.006	0.294
	0.25			20.85	18.29	19.631	60.887		0.857	-0.983	-0.913	0.306
	0.30			20.84	19.11	23.040	68.083		0.958	-0.938	-0.931	0.328
$^{70}\text{Yb}_{104}^{174}$	0.20	763	685	20.30	17.36	16.850	54.162	73.74	0.734	-1.076	-0.754	0.273
	0.25			20.84	18.55	20.226	62.121		0.842	-1.015	-0.667	0.292
	0.30			20.84	19.95	23.614	68.942		0.934	-0.962	-0.664	0.315
$^{70}\text{Yb}_{106}^{176}$	0.20	744	675	20.31	17.73	17.335	53.350	68.41	0.780	-1.112	-0.399	0.258
	0.25			20.87	18.69	20.717	59.310		0.867	-1.042	-0.447	0.298
	0.30			20.87	18.53	24.086	68.529		1.002	-0.981	-0.430	0.310
$^{72}\text{Hf}_{102}^{174}$	0.20	852	705	20.96	17.31	13.027	48.903			-0.657	-0.999	0.283
	0.25			20.90	18.47	16.397	57.496			-0.663	-0.908	0.293
	0.30			20.39	19.29	22.972	67.905			-0.554	-0.927	0.353
$^{72}\text{Hf}_{104}^{176}$	0.20	832	709	20.99	17.69	13.390	49.209	67.5	0.729	-0.680	-0.712	0.264
	0.25			20.93	18.87	16.765	57.304		0.849	-0.681	-0.637	0.281
	0.30			20.40	19.27	23.465	67.709		1.003	-0.562	-0.639	0.345
$^{72}\text{Hf}_{106}^{178}$	0.20	812	709	21.01	18.12	13.771	47.938	64.1	0.748	-0.703	-0.363	0.249
	0.25			20.96	19.07	17.147	54.273		0.847	-0.699	-0.416	0.286
	0.30			20.40	18.96	23.975	67.063		1.046	-0.569	-0.405	0.342

Table 1b continued

$Z X_N^A$	$\varepsilon$	$\Delta_p$ (keV)	$\Delta_h$ (keV)	$G_p$ XA	$G_h$ XA	$\frac{2}{\hbar^2} J_p$ (MeV) $^{-1}$	$\frac{2}{\hbar^2} J$ (MeV) $^{-1}$	$\frac{2}{\hbar^2} J_{\text{exp}}$ (MeV) $^{-1}$	$F = \frac{J}{J_{\text{exp}}}$	$\frac{2}{\hbar^2} W_p$ (MeV) $^{-1}$	$\frac{2}{\hbar^2} W_n$ (MeV) $^{-1}$	$g_R$
$^{72}\text{Hf}_{108}^{180}$	0.20	795	746	21.05	18.60	14.108	44.670	64.1	0.697	-0.724	-0.123	0.252
	0.25			21.00	19.30	17.484	51.912		0.810	-0.716	-0.311	0.296
	0.30			20.43	19.22	24.423	69.330		1.082	-0.576	-0.186	0.324
$^{74}\text{W}_{106}^{180}$	0.20	826	719	21.52	18.34	11.234	44.870			-0.392	-0.353	0.240
	0.25			20.72	19.30	14.578	51.298			-0.433	-0.408	0.276
	0.30			19.77	19.20	25.739	68.469			-0.241	-0.398	0.382
$^{74}\text{W}_{108}^{182}$	0.20	800	765	21.51	18.88	11.590	41.313	60.0	0.689	-0.408	-0.117	0.246
	0.25			20.69	19.57	14.916	48.643		0.811	-0.447	-0.300	0.288
	0.30			19.70	19.52	26.554	70.591		1.177	-0.236	-0.185	0.371
$^{74}\text{W}_{110}^{184}$	0.20	783	787	21.56	18.95	11.834	38.181	54.1	0.706	-0.419	-0.126	0.272
	0.25			20.73	19.11	15.149	48.057		0.888	-0.457	-0.386	0.302
	0.30			17.70	19.72	27.112	75.877		1.403	-0.233	-0.178	0.352
$^{74}\text{W}_{112}^{186}$	0.20	764	751	21.60	18.50	12.116	35.603	49.0	0.727	-0.432	-0.265	0.313
	0.25			20.75	18.18	15.414	49.631		1.013	-0.469	-0.543	0.309
	0.30			19.68	19.02	27.757	80.857		1.650	-0.228	-0.433	0.351
$^{76}\text{Os}_{108}^{186}$	0.20	815	722	21.91	18.75	10.226	41.860			-0.251	-0.129	0.229
	0.25			20.52	19.47	14.571	49.983			-0.248	-0.324	0.294
	0.30			19.42	19.36	28.948	75.096			-0.056	-0.190	0.392

Table 1b continued

$Z X_N^A$	$\varepsilon$	$\Delta_p$ (keV)	$\Delta_h$ (keV)	$G_p$ XA	$G_h$ XA	$\frac{2}{\hbar^2} J_p$ (MeV) $^{-1}$	$\frac{2}{\hbar^2} J$ (MeV) $^{-1}$	$\frac{2}{\hbar^2} J_{\text{exp}}$ (MeV) $^{-1}$	$F = \frac{J}{J_{\text{exp}}}$	$\frac{2}{\hbar^2} W_p$ (MeV) $^{-1}$	$\frac{2}{\hbar^2} W_n$ (MeV) $^{-1}$	$g_R$
$^{76}\text{Os}_{110}^{186}$	0.20	780	748	21.90	18.83	10.650	38.508	42.8	0.900	-0.268	-0.134	0.258
	0.25			20.42	19.96	15.007	49.467		1.156	-0.259	-0.414	0.311
	0.30			19.24	19.62	30.344	81.686		1.909	-0.040	-0.174	0.377
$^{76}\text{Os}_{112}^{188}$	0.20	743	742	21.87	18.58	11.129	34.894	37.5	0.931	-0.288	-0.268	0.310
	0.25			20.30	18.25	15.481	50.095		1.336	-0.271	-0.550	0.326
	0.30			19.03	19.10	31.944	85.671		2.285	-0.021	-0.437	0.391
$^{76}\text{Os}_{114}^{190}$	0.20	722	668	21.92	17.92	11.418	33.230	30.61	1.086	-0.300	-0.528	0.363
	0.25			20.30	17.20	15.766	54.818		1.791	-0.279	-0.779	0.319
	0.30			18.98	17.85	32.912	90.914		2.970	-0.010	-0.857	0.398
$^{76}\text{Os}_{116}^{192}$	0.20	711	537	22.03	17.11	11.577	34.548			-0.306	-0.955	0.400
	0.25			20.38	15.79	15.929	65.661			-0.283	-1.123	0.288
	0.30			19.02	16.13	33.436	101.522			-0.004	-1.369	0.381

Table 2a

Moment of inertia and collective gyromagnetic ratio of some of the doubly even nuclei for the gap parameters  $\Delta_p = P_p$  and  $\Delta_h = P_h$

$Z X_N^A$	$\varepsilon$	$\Delta_p$ (keV)	$\Delta_h$ (keV)	$G_p$ XA	$G_h$ XA	$\frac{2}{\hbar^2} J_p$ (MeV) $^{-1}$	$\frac{2}{\hbar^2} J$ (MeV) $^{-1}$	$\frac{2}{\hbar^2} J_{\text{exp}}$ (MeV) $^{-1}$	$F = \frac{J}{J_{\text{exp}}}$	$\frac{2}{\hbar^2} W_p$ (MeV) $^{-1}$	$\frac{2}{\hbar^2} W_n$ (MeV) $^{-1}$	$g_R$
$^{62}\text{Sm}_{90}^{152}$	0.20	1100	1110	21.51	18.19	11.959	26.757	47.3	0.566	-0.759	-0.644	0.409
	0.25			22.63	18.21	15.338	38.060		0.805	-0.938	-1.038	0.394
	0.30			23.54	18.54	18.136	49.297		1.042	-1.063	-1.454	0.382
$^{62}\text{Sm}_{92}^{154}$	0.20	1100	1000	21.73	17.59	11.930	31.698	73.2	0.433	-0.757	-0.908	0.376
	0.25			22.86	17.89	15.315	42.560		0.581	-0.936	-1.292	0.375
	0.30			23.77	18.23	18.125	52.559		0.718	-1.061	-1.642	0.372
$^{64}\text{Gd}_{90}^{154}$	0.20	1020	1110	20.97	18.38	13.791	28.555	48.8	0.585	-0.905	-0.643	0.424
	0.25			22.03	18.40	16.785	39.464		0.809	-1.073	-1.035	0.401
	0.30			22.74	18.73	19.321	50.441		1.034	-1.209	-1.451	0.383
$^{64}\text{Gd}_{92}^{156}$	0.20	1020	1000	21.18	17.77	13.764	33.487	66.7	0.502	-0.903	-0.906	0.391
	0.25			22.25	18.07	16.767	43.970		0.659	-1.071	-1.290	0.382
	0.30			22.97	18.42	19.314	53.727		0.806	-1.208	-1.640	0.373
$^{64}\text{Gd}_{94}^{158}$	0.20	1020	950	21.39	17.60	13.738	36.954	75.0	0.493	-0.901	-1.104	0.374
	0.25			22.47	18.16	16.749	46.084		0.614	-1.070	-1.417	0.375
	0.30			23.19	18.44	19.308	54.769		0.730	-1.206	-1.717	0.371
$^{64}\text{Gd}_{96}^{160}$	0.20	1020	940	21.61	17.77	13.712	38.765	79.7	0.486	-0.899	-1.166	0.362
	0.25			22.68	18.56	16.732	47.276		0.593	-1.068	-1.462	0.369
	0.30			23.41	18.85	19.301	54.872		0.688	-1.205	-1.709	0.370

Table 2a continued

$zX_N^A$	$\varepsilon$	$\Delta_p$ (keV)	$\Delta_h$ (keV)	$G_p$ XA	$G_h$ XA	$\frac{2}{\hbar^2} J_p$ (MeV) $^{-1}$	$\frac{2}{\hbar^2} J$ (MeV) $^{-1}$	$\frac{2}{\hbar^2} J_{\text{exp}}$ (MeV) $^{-1}$	$F = \frac{J}{J_{\text{exp}}}$	$\frac{2}{\hbar^2} W_p$ (MeV) $^{-1}$	$\frac{2}{\hbar^2} W_n$ (MeV) $^{-1}$	$g_R$
$^{66}\text{Dy}_{94}^{160}$	0.20	960	905	21.09	17.48	15.120	40.003	68.5	0.584	-0.996	-1.184	0.377
	0.25			22.10	18.05	17.878	48.992		0.715	-1.126	-1.507	0.377
	0.30			22.57	18.33	19.767	57.075		0.833	-1.227	-1.815	0.369
	0.20	960	940	21.29	17.94	15.093	40.099	74.0	0.542	-0.994	-1.163	0.374
	0.25			22.31	18.73	17.863	48.379		0.654	-1.125	-1.460	0.378
	0.30			22.78	19.03	19.770	55.330		0.748	-1.226	-1.707	0.374
$^{66}\text{Dy}_{98}^{162}$	0.20	960	900	21.49	17.93	15.066	42.650	80.8	0.528	-0.992	-1.173	0.352
	0.25			22.52	18.91	17.849	50.770		0.628	-1.123	-1.422	0.357
	0.30			22.99	19.29	19.772	56.111		0.694	-1.225	-1.553	0.358
	0.20	960	800	21.69	17.40	15.039	46.642			-0.990	-1.136	0.318
	0.25			22.73	18.46	17.834	54.243			-1.121	-1.203	0.319
	0.30			23.20	19.05	19.773	59.153			-1.224	-1.247	0.320
$^{66}\text{Er}_{96}^{164}$	0.20	900	940	20.78	18.12	15.266	40.226	66.7	0.603	-1.005	-1.161	0.375
	0.25			21.63	18.91	17.946	48.433		0.726	-1.041	-1.457	0.387
	0.30			21.91	19.21	19.872	55.422		0.831	-1.094	-1.705	0.386
	0.20	900	900	20.97	18.09	15.250	42.784	74.1	0.574	-1.003	-1.170	0.354
	0.25			21.83	19.08	17.945	50.836		0.682	-1.041	-1.419	0.366
	0.30			22.11	19.47	19.888	56.228		0.755	-1.094	-1.551	0.370

Table 2a continued

$zX_N^A$	$\varepsilon$	$\Delta_p$ (keV)	$\Delta_h$ (keV)	$G_p$ XA	$G_h$ XA	$\frac{2}{\hbar^2} J_p$ (MeV) $^{-1}$	$\frac{2}{\hbar^2} J$ (MeV) $^{-1}$	$\frac{2}{\hbar^2} J_{\text{exp}}$ (MeV) $^{-1}$	$F = \frac{J}{J_{\text{exp}}}$	$\frac{2}{\hbar^2} W_p$ (MeV) $^{-1}$	$\frac{2}{\hbar^2} W_n$ (MeV) $^{-1}$	$g_R$
$^{68}\text{Er}_{100}^{168}$	0.20	900	800	21.17	17.56	15.234	46.804	75.0	0.624	-1.002	-1.134	0.320
	0.25			22.02	18.63	17.944	54.349		0.725	-1.040	-1.202	0.327
	0.30			22.31	19.22	19.903	59.311		0.791	-1.094	-1.247	0.331
	0.20	900	700	21.36	16.96	15.218	51.418	75.6	0.680	-1.000	-1.011	0.282
	0.25			22.22	18.11	17.942	59.299		0.784	-1.039	-0.916	0.281
	0.30			22.51	18.93	19.918	65.021		0.860	-1.094	-0.933	0.284
$^{70}\text{Yb}_{98}^{168}$	0.20	830	900	20.30	18.26	15.293	42.779			-0.959	-1.168	0.359
	0.25			20.80	19.26	18.628	51.489			-0.929	-1.416	0.384
	0.30			20.79	19.65	22.054	58.394			-0.897	-1.549	0.409
	0.20	830	800	20.49	17.72	15.281	46.820	66.36	0.706	-0.958	-1.132	0.325
	0.25			20.99	18.79	18.628	55.029		0.829	-0.929	-1.201	0.345
	0.30			20.98	19.39	22.070	61.506		0.927	-0.898	-1.246	0.369

Table 2b

Moment of inertia and collective gyromagnetic ratio of some of the doubly even nuclei for the gap parameters  $\Delta_p = P_p$  and  $\Delta_n = P_n$

$Z X_N^A$	$\epsilon$	$\Delta_p$ (keV)	$\Delta_h$ (keV)	$G_p$ XA	$G_h$ XA	$\frac{2}{\hbar^2} J_p$ (MeV) $^{-1}$	$\frac{2}{\hbar^2} J$ (MeV) $^{-1}$	$\frac{2}{\hbar^2} J_{\text{exp}}$ (MeV) $^{-1}$	$F = \frac{J}{J_{\text{exp}}}$	$\frac{2}{\hbar^2} W_p$ (MeV) $^{-1}$	$\frac{2}{\hbar^2} W_n$ (MeV) $^{-1}$	$g_R$
$^{70}\text{Yb}_{102}^{172}$	0.20	830	700	20.68	17.11	15.269	51.452	71.07	0.724	-0.956	-1.010	0.287
	0.25			21.18	18.27	18.628	59.995		0.844	-0.928	-0.916	0.298
	0.30			21.17	19.09	22.087	67.230		0.946	-0.898	-0.933	0.320
$^{70}\text{Yb}_{104}^{174}$	0.20	830	685	20.86	17.36	15.257	52.568	73.74	0.713	-0.954	-0.754	0.262
	0.25			21.37	18.55	18.627	60.523		0.821	-0.928	-0.667	0.280
	0.25	830	685	21.37	18.55	18.627	60.523	73.74	0.821	-0.928	-0.667	0.280
	0.30			21.36	18.95	22.102	67.431		0.914	-0.899	-0.664	0.304
$^{70}\text{Yb}_{106}^{176}$	0.20	830	740	21.05	18.17	15.245	47.852	68.41	0.699	-0.952	-0.337	0.254
	0.25			21.55	19.11	18.627	54.425		0.796	-0.927	-0.393	0.292
	0.30			21.55	19.04	22.118	63.906		0.934	-0.899	-0.384	0.305
$^{72}\text{Hf}_{102}^{174}$	0.20	780	700	20.38	17.27	14.451	50.617			-0.748	-1.008	0.294
	0.25			20.35	18.43	17.759	59.136			-0.731	-0.915	0.303
	0.30			19.76	19.26	24.767	69.949			-0.577	-0.934	0.367
$^{72}\text{Hf}_{104}^{176}$	0.20	780	685	20.56	17.51	14.443	51.732	67.5	0.766	-0.747	-0.752	0.269
	0.25			20.52	18.71	17.768	59.671		0.884	-0.731	-0.666	0.284
	0.30			19.94	19.11	24.783	70.160		1.039	-0.578	-0.664	0.352

Table 2b continued

$Z X_N^A$	$\epsilon$	$\Delta_p$ (keV)	$\Delta_h$ (keV)	$G_p$ XA	$G_h$ XA	$\frac{2}{\hbar^2} J_p$ (MeV) $^{-1}$	$\frac{2}{\hbar^2} J$ (MeV) $^{-1}$	$\frac{2}{\hbar^2} J_{\text{exp}}$ (MeV) $^{-1}$	$F = \frac{J}{J_{\text{exp}}}$	$\frac{2}{\hbar^2} W_p$ (MeV) $^{-1}$	$\frac{2}{\hbar^2} W_n$ (MeV) $^{-1}$	$g_R$
$^{72}\text{Hf}_{106}^{178}$	0.20	780	740	20.74	18.33	14.434	47.027	64.1	0.734	-0.746	-0.336	0.262
	0.25			20.70	19.27	17.775	53.594		0.836	-0.731	-0.392	0.297
	0.30			20.12	19.20	24.799	66.634		1.040	-0.580	-0.384	0.354
$^{72}\text{Hf}_{108}^{180}$	0.20	780	660	20.92	18.04	14.425	49.094	64.1	0.766	-0.744	-0.155	0.236
	0.25			20.88	18.78	17.783	55.686		0.869	-0.731	-0.365	0.284
	0.30			20.29	18.55	24.815	74.047		1.155	-0.581	-0.197	0.309
$^{74}\text{W}_{106}^{180}$	0.20	830	740	21.55	18.48	11.181	43.760			-0.389	-0.335	0.244
	0.25			20.75	19.43	14.529	50.367			-0.431	-0.391	0.279
	0.30			19.81	19.37	25.617	67.498			-0.242	-0.384	0.385
	0.20	830	660	21.73	18.19	11.182	45.853	60.0	0.764	-0.389	-0.154	0.218
	0.25			20.93	18.93	14.545	52.485		0.875	-0.431	-0.365	0.266
	0.30			19.98	18.70	25.619	74.904		1.248	-0.244	-0.198	0.337
$^{74}\text{W}_{110}^{184}$	0.20	830	825	21.91	19.22	11.182	36.151	51.1	0.668	-0.388	-0.119	0.273
	0.25			21.11	19.41	14.562	46.049		0.851	-0.430	-0.361	0.303
	0.30			20.16	19.98	25.621	72.047		1.332	-0.246	-0.183	0.350
$^{74}\text{W}_{112}^{186}$	0.20	830	820	22.09	19.06	11.183	32.691	49.0	0.688	-0.388	-0.243	0.316
	0.25			21.28	18.82	14.577	46.007		0.939	-0.430	-0.488	0.314
	0.30			20.33	19.58	25.622	74.238		1.561	-0.247	-0.407	0.351

Table 2b continued

$zX_N^A$	$\varepsilon$	$\Delta_p$ (keV)	$\Delta_h$ (keV)	$G_p$ XA	$G_h$ XA	$\frac{2}{\hbar^2} J_p$ (MeV) $^{-1}$	$\frac{2}{\hbar^2} J$ (MeV) $^{-1}$	$\frac{2}{\hbar^2} J_{\text{exp}}$ (MeV) $^{-1}$	$F = \frac{J}{J_{\text{exp}}}$	$\frac{2}{\hbar^2} W_p$ (MeV) $^{-1}$	$\frac{2}{\hbar^2} W_n$ (MeV) $^{-1}$	$g_R$
$^{76}\text{Os}_{108}^{184}$	0.20	960	660	22.72	18.34	8.730	43.404			-0.196	-0.154	0.194
	0.25			21.59	19.08	12.959	50.933			-0.213	-0.365	0.263
	0.30			20.76	18.86	24.098	73.435			-0.110	-0.198	0.332
$^{76}\text{Os}_{110}^{186}$	0.20	960	825	22.91	19.38	8.730	33.684	42.80	0.787	-0.196	-0.119	0.246
	0.25			21.77	19.57	12.969	44.462		1.039	-0.213	-0.360	0.301
	0.30			20.95	20.14	24.084	70.501		1.647	-0.111	-0.183	0.344
$^{76}\text{Os}_{112}^{188}$	0.20	960	820	23.09	19.22	8.730	30.236	37.5	0.806	-0.195	-0.243	0.290
	0.25			21.95	18.98	12.979	44.410		1.184	-0.213	-0.487	0.312
	0.30			21.13	19.75	24.071	72.680		1.938	-0.112	-0.408	0.346
$^{76}\text{Os}_{114}^{190}$	0.20	960	910	23.27	20.00	8.730	25.434	30.61	0.831	-0.195	-0.392	0.367
	0.25			22.13	19.56	12.989	41.229		1.347	-0.213	-0.557	0.343
	0.30			21.31	20.17	24.058	67.258		2.197	-0.114	-0.624	0.385
$^{76}\text{Os}_{116}^{192}$	0.20	960	950	23.46	20.58	8.730	23.747			-0.195	-0.554	0.419
	0.25			23.31	19.99	12.999	40.198			-0.213	-0.667	0.363
	0.30			21.49	20.49	24.045	64.975			-0.115	-0.794	0.409

Table 3a

Moment of inertia and collective gyromagnetic ratio of some of the doubly even nuclei for the gap parameters  $\Delta_p = 12\sqrt{A}$  and  $\Delta_h = 11.2/\sqrt{A}$ .

$zX_N^A$	$\varepsilon$	$\Delta_p$ (keV)	$\Delta_h$ (keV)	$G_p$ XA	$G_h$ XA	$\frac{2}{\hbar^2} J_p$ (MeV) $^{-1}$	$\frac{2}{\hbar^2} J$ (MeV) $^{-1}$	$\frac{2}{\hbar^2} J_{\text{exp}}$ (MeV) $^{-1}$	$F = \frac{J}{J_{\text{exp}}}$	$\frac{2}{\hbar^2} W_p$ (MeV) $^{-1}$	$\frac{2}{\hbar^2} W_n$ (MeV) $^{-1}$	$g_R$
$^{62}\text{Sm}_{90}^{152}$	0.20	973	908	20.57	16.95	14.401	34.401	47.3	0.727	-0.929	-0.836	0.388
	0.25			21.76	16.95	18.000	48.031		1.015	-1.115	-1.391	0.379
	0.30			22.73	17.38	20.721	60.748		1.284	-1.226	-1.925	0.370
$^{62}\text{Sm}_{94}^{154}$	0.20	967	903	20.73	16.97	14.511	37.585	73.2	0.513	-0.936	-1.051	0.379
	0.25			21.94	17.28	18.129	49.390		0.675	-1.123	-1.490	0.378
	0.30			22.91	17.64	20.859	59.431		0.812	-1.234	-1.855	0.375
$^{64}\text{Gd}_{90}^{154}$	0.20	967	903	20.59	17.09	14.887	35.039	48.8	0.718	-0.980	-0.842	0.389
	0.25			21.67	17.08	17.919	48.170		0.987	-1.152	-1.401	0.374
	0.30			22.40	17.52	20.447	60.731		1.244	-1.288	-1.939	0.361
$^{64}\text{Gd}_{92}^{156}$	0.20	961	897	20.76	17.10	14.996	38.244	66.7	0.573	-0.987	-1.059	0.380
	0.25			21.84	17.42	18.044	49.529		0.743	-1.161	-1.501	0.373
	0.30			22.58	17.78	20.582	59.409		0.891	-1.397	-1.867	0.367
$^{64}\text{Gd}_{94}^{158}$	0.20	955	891	20.92	17.22	15.105	40.606	75.0	0.541	-0.995	-1.214	0.374
	0.25			22.02	17.79	18.167	49.904		0.665	-1.169	-1.539	0.375
	0.30			22.76	18.06	20.715	58.629		0.782	-1.306	-1.847	0.372
$^{64}\text{Gd}_{96}^{160}$	0.20	949	885	21.08	17.43	15.214	42.505	79.7	0.533	-1.002	-1.278	0.365
	0.25			22.19	18.23	18.289	51.119		0.641	-1.177	-1.588	0.371
	0.30			22.93	18.51	20.848	58.722		0.737	-1.315	-1.845	0.373

Table 3a continued

$zX_N^A$	$\varepsilon$	$\Delta_p$ (keV)	$\Delta_h$ (keV)	$G_p$ XA	$G_h$ XA	$\frac{2}{\hbar^2} J_p$ (MeV) $^{-1}$	$\frac{2}{\hbar^2} J$ (MeV) $^{-1}$	$\frac{2}{\hbar^2} J_{\text{exp}}$ (MeV) $^{-1}$	$F = \frac{J}{J_{\text{exp}}}$	$\frac{2}{\hbar^2} W_p$ (MeV) $^{-1}$	$\frac{2}{\hbar^2} W_n$ (MeV) $^{-1}$	$g_R$
$^{66}\text{Dy}_{94}^{160}$	0.20	949	885	21.01	17.35	15.379	41.064	68.5	0.599	-1.014	-1.223	0.375
	0.25			22.03	17.93	18.132	50.084		0.731	-1.144	-1.549	0.376
	0.30			22.50	18.20	19.996	58.151		0.849	-1.244	-1.859	0.368
$^{66}\text{Dy}_{96}^{162}$	0.20	943	880	21.17	17.56	15.488	42.973	74	0.581	-1.022	-1.288	0.366
	0.25			22.20	18.37	18.252	51.299		0.693	-1.152	-1.599	0.372
	0.30			22.67	18.66	20.119	58.232		0.787	-1.252	-1.857	0.369
$^{66}\text{Dy}_{98}^{164}$	0.20	937	875	21.33	17.77	15.597	44.336	80.8	0.549	-1.029	-1.229	0.351
	0.25			22.37	18.76	18.372	52.461		0.649	-1.160	-1.484	0.357
	0.30			22.84	19.14	20.241	57.623		0.713	-1.260	-1.612	0.358
$^{66}\text{Dy}_{100}^{166}$	0.20	931	869	21.49	17.86	15.705	44.111			-1.037	-1.006	0.336
	0.25			22.54	18.90	18.490	51.838			-1.168	-1.084	0.333
	0.30			23.02	19.47	20.363	57.053			-1.268	-1.139	0.331
$^{68}\text{Er}_{96}^{164}$	0.20	937	875	21.04	17.70	14.501	42.178	66.7	0.632	-0.948	-1.297	0.358
	0.25			21.87	18.51	17.216	50.478		0.757	-0.993	-1.610	0.373
	0.30			22.15	18.80	19.227	57.577		0.863	-1.049	-1.870	0.375
$^{68}\text{Er}_{98}^{166}$	0.20	931	869	21.20	17.90	15.598	43.536	74.1	0.588	-0.955	-1.237	0.343
	0.25			22.03	18.90	17.322	51.632		0.697	-0.999	-1.494	0.357
	0.30			22.31	19.29	19.337	56.944		0.768	-1.056	-1.623	0.364

Table 3a continued

$zX_N^A$	$\varepsilon$	$\Delta_p$ (keV)	$\Delta_h$ (keV)	$G_p$ XA	$G_h$ XA	$\frac{2}{\hbar^2} J_p$ (MeV) $^{-1}$	$\frac{2}{\hbar^2} J$ (MeV) $^{-1}$	$\frac{2}{\hbar^2} J_{\text{exp}}$ (MeV) $^{-1}$	$F = \frac{J}{J_{\text{exp}}}$	$\frac{2}{\hbar^2} W_p$ (MeV) $^{-1}$	$\frac{2}{\hbar^2} W_n$ (MeV) $^{-1}$	$g_R$
$^{68}\text{Er}_{100}^{168}$	0.20	926	864	21.35	17.99	14.694	43.288	75.0	0.577	-0.962	-1.013	0.327
	0.25			22.20	19.04	17.427	50.982		0.680	-1.006	-1.091	0.333
	0.30			22.48	19.62	19.447	56.349		0.751	-1.062	-1.146	0.336
$^{68}\text{Er}_{102}^{170}$	0.20	920	859	21.51	18.13	14.789	43.139	75.6	0.571	-0.968	-0.759	0.307
	0.25			22.36	19.20	17.532	51.152		0.677	-1.012	-0.725	0.306
	0.30			22.65	19.88	19.556	57.513		0.761	-1.069	-0.760	0.305
$^{70}\text{Yb}_{98}^{168}$	0.20	926	864	21.04	18.03	13.369	42.506			-0.815	-1.246	0.339
	0.25			21.49	19.04	16.642	51.173			-0.820	-1.504	0.364
	0.30			21.49	19.43	20.107	57.938			-0.814	-1.634	0.390
$^{70}\text{Yb}_{100}^{170}$	0.20	920	859	21.19	18.12	13.459	42.238	66.36	0.636	-0.821	-1.020	0.322
	0.25			21.65	19.18	16.743	50.502		0.761	-0.825	-1.098	0.340
	0.30			21.65	19.76	20.221	57.334		0.864	-0.819	-1.153	0.364

Table 3b

Moment of inertia and collective gyromagnetic ratio of some of the doubly even nuclei for the gap parameters  $\Delta_p = 12\sqrt{A}$  and  $\Delta_n = 11.2/\sqrt{A}$ .

$Z X_N^A$	$\epsilon$	$\Delta_p$ (keV)	$\Delta_h$ (keV)	$G_p$ XA	$G_h$ XA	$\frac{2}{\hbar^2} J_p$ (MeV) $^{-1}$	$\frac{2}{\hbar^2} J$ (MeV) $^{-1}$	$\frac{2}{\hbar^2} J_{\text{exp}}$ (MeV) $^{-1}$	$F = \frac{J}{J_{\text{exp}}}$	$\frac{2}{\hbar^2} W_p$ (MeV) $^{-1}$	$\frac{2}{\hbar^2} W_n$ (MeV) $^{-1}$	$g_R$
$^{70}\text{Yb}_{102}^{172}$	0.20	915	854	21.35	18.26	13.541	42.072	71.07	0.592	-0.826	-0.765	0.301
	0.25			21.81	19.34	16.843	50.665		0.713	-0.830	-0.730	0.312
	0.30			21.80	20.02	20.335	58.509		0.823	-0.824	-0.764	0.333
$^{70}\text{Yb}_{104}^{174}$	0.20	910	848	21.50	18.53	13.627	42.335	73.74	0.574	-0.832	-0.528	0.279
	0.25			21.96	19.60	16.943	50.605		0.686	-0.835	-0.500	0.297
	0.30			21.96	20.01	20.448	58.645		0.795	-0.828	-0.518	0.318
$^{70}\text{Yb}_{106}^{176}$	0.20	905	844	21.65	18.85	13.712	41.68	68.41	0.609	-0.837	-0.267	0.261
	0.25			22.12	19.76	17.042	48.843		0.714	-0.840	-0.325	0.296
	0.30			22.12	19.80	20.561	58.411		0.854	-0.833	-0.325	0.308
$^{72}\text{Hf}_{102}^{174}$	0.20	910	849	21.40	18.39	12.039	40.749			-0.596	-0.770	0.301
	0.25			21.33	19.48	15.410	49.433			-0.615	-0.734	0.311
	0.30			20.87	20.17	21.651	60.039			-0.534	-0.769	0.369
$^{72}\text{Hf}_{104}^{176}$	0.20	905	844	21.55	18.66	12.113	41.001	67.5	0.607	-0.600	-0.532	0.278
	0.25			21.48	19.74	15.497	49.357		0.731	-0.619	-0.503	0.295
	0.30			21.02	20.15	21.772	60.178		0.892	-0.539	-0.521	0.354
$^{72}\text{Hf}_{106}^{178}$	0.20	899	839	21.70	18.98	12.186	40.327	64.1	0.629	-0.604	-0.269	0.259
	0.25			21.63	19.90	15.512	48.825		0.762	-0.618	-0.305	0.280
	0.30			21.16	19.94	21.892	59.943		0.935	-0.539	-0.327	0.345

Table 3b continued

$Z X_N^A$	$\epsilon$	$\Delta_p$ (keV)	$\Delta_h$ (keV)	$G_p$ XA	$G_h$ XA	$\frac{2}{\hbar^2} J_p$ (MeV) $^{-1}$	$\frac{2}{\hbar^2} J$ (MeV) $^{-1}$	$\frac{2}{\hbar^2} J_{\text{exp}}$ (MeV) $^{-1}$	$F = \frac{J}{J_{\text{exp}}}$	$\frac{2}{\hbar^2} W_p$ (MeV) $^{-1}$	$\frac{2}{\hbar^2} W_n$ (MeV) $^{-1}$	$g_R$
$^{72}\text{Hf}_{108}^{180}$	0.20	894	835	21.85	19.17	12.259	39.180	64.1	0.611	-0.607	-0.104	0.252
	0.25			21.78	19.83	15.670	46.879		0.731	-0.626	-0.267	0.295
	0.30			21.31	19.87	22.011	62.887		0.981	-0.542	-0.177	0.321
$^{74}\text{W}_{106}^{180}$	0.20	894	835	21.99	19.11	10.376	38.686			-0.353	-0.271	0.253
	0.25			21.24	20.04	13.771	45.924			-0.398	-0.330	0.288
	0.30			20.40	20.07	23.775	62.024			-0.255	-0.329	0.385
$^{74}\text{W}_{108}^{182}$	0.20	889	830	22.14	19.30	10.434	37.512	60.0	0.625	-0.355	-0.105	0.245
	0.25			21.39	19.97	13.841	45.217		0.754	-0.400	-0.269	0.288
	0.30			20.54	20.00	23.907	64.999		1.083	-0.256	-0.178	0.360
$^{74}\text{W}_{110}^{184}$	0.20	885	826	22.29	19.23	10.492	35.436	54.1	0.655	-0.357	-0.119	0.263
	0.25			21.53	19.41	13.910	45.373		0.839	-0.402	-0.360	0.296
	0.30			20.67	19.98	24.039	70.424		1.302	-0.256	-0.183	0.335
$^{74}\text{W}_{112}^{186}$	0.20	880	821	22.44	19.07	10.549	32.024	49.0	0.654	-0.359	-0.243	0.307
	0.25			21.67	18.83	13.979	45.362		0.926	-0.405	-0.487	0.308
	0.30			20.81	19.60	24.170	72.710		1.484	-0.257	-0.407	0.338
$^{76}\text{Os}_{108}^{184}$	0.20	885	826	22.30	19.43	9.462	36.697			-0.222	-0.105	0.241
	0.25			21.03	20.11	13.773	45.317			-0.230	-0.271	0.304
	0.30			20.08	21.14	26.442	67.750			-0.085	-0.179	0.395

Table 3b continued

$Z X_N^A$	$\epsilon$	$\Delta_p$ (keV)	$\Delta_h$ (keV)	$G_p$ XA	$G_h$ XA	$\frac{2}{\hbar^2} J_p$ (MeV) $^{-1}$	$\frac{2}{\hbar^2} J$ (MeV) $^{-1}$	$\frac{2}{\hbar^2} J_{\text{exp}}$ (MeV) $^{-1}$	$F = \frac{J}{J_{\text{exp}}}$	$\frac{2}{\hbar^2} W_p$ (MeV) $^{-1}$	$\frac{2}{\hbar^2} W_n$ (MeV) $^{-1}$	$g_R$
$^{76}\text{Os}_{110}^{186}$	0.20	880	821	22.45	19.36	9.512	34.599	42.80	0.808	-0.223	-0.119	0.259
	0.25			21.18	19.54	13.841	45.472		1.062	-0.231	-0.363	0.312
	0.30			20.21	20.11	26.591	73.233		1.711	-0.085	-0.183	0.367
	0.20	875	817	22.60	19.19	9.563	31.154	37.5	0.831	-0.225	-0.244	0.304
	0.25			21.31	18.95	13.908	45.459		1.212	-0.232	-0.489	0.324
	0.30			20.34	19.72	26.739	75.543		2.014	-0.085	-0.409	0.370
	0.20	871	813	22.75	19.21	9.613	28.155	30.61	0.920	-0.226	-0.440	0.364
	0.25			21.45	18.67	13.975	45.918		1.500	-0.233	-0.634	0.334
	0.30			20.47	19.30	26.886	75.427		2.464	-0.084	-0.706	0.384
	0.20	866	808	22.91	19.51	9.663	26.964			-0.227	-0.668	0.414
	0.25			21.59	18.69	14.041	46.678			-0.234	-0.793	0.343
	0.30			20.60	19.17	27.033	75.406			-0.084	-0.947	0.401

In the tables given above the nuclei are shown in the first column and the values of the deformation parameter are given in the second. The third and the fourth columns are the gap parameters for protons and neutrons, respectively. The following two columns present the pairing energy times the mass number for the same nucleons, whereas the seventh is the column representing the contribution of the protons to the moment of inertia of the nucleus, which is given in equation (21). In column eight the calculated total momenta of inertia of the nuclei are listed, the neighbouring column represents the experimental values taken from refs. [7—9]. The tenth column shows the ratio of the calculated to the experimental moment of inertia. The next two columns are the  $W_i$  values of the formula (21) for protons and neutrons, respectively. In the last column calculated gyromagnetic ratios are given.

The comparison between experiment and theory shows a very good agreement for  $\text{Sm}^{152}$ ,  $\text{Gd}^{154}$ ,  $\text{Er}^{164}$ ,  $\text{Er}^{166}$ , all Yb and Hf isotopes,  $W^{186}$  and Os isotopes. In the case of the Dy, Gd and W isotopes the theoretical values do not differ much from the experimental ones and the agreement is rather good.

## VI. CONCLUSIONS

The theoretical results obtained according to three alternative procedures described in the preceding section are consistent with each other and in general show good agreement with the experimental data.

The choice of an alternative basis, namely an asymptotic basis in the calculations improves somewhat the accuracy of the theoretical predictions.

One can see the dependence of the moment of inertia and the gyromagnetic ratio on the deformation parameter by taking into account three different values of  $\epsilon$  in the calculations. Considering the change of  $\epsilon$  in different intervals for different nuclei and performing the same calculation, it seems possible to find the exact experimental results given for each nucleus. Thus this procedure reveals a theoretical prediction for the deformation degree of the nuclei.

## REFERENCES

- [1] Lamm, I. L. Nucl. Phys. *A125* (1969), 504.
- [2] Boisson, J. P., Piepenbring, R. Nucl. Phys. *A168* (1971), 385.
- [3] Bogolyubov, N. N., Nuovo Cimento *7* (1958), 794; Valantin, J. G. Nuovo Cimento *7* (1958), 843.
- [4] Belyaev, S. T. Mat. Fys. Medd. Dan. Vid. Selsk. *31* no. 11 (1959).
- [5] Eisenberg, J. M., Greiner, W. *Nuclear Theory*, vol. 3 North-Holland Amsterdam, 1976.
- [6] Prior, O., Boehm, F., Nilsson, S. G. Nucl. Phys. *A110* (1968), 257.
- [7] Marklund, I., Von Noijen, B., Grabowski, Z. Nucl. Phys. *15* (1960), 533.

- [8] Strominger, D., Hollander, J. M., Seaborg, G. T. Rev. Mod. Phys. 30 (1958), 585.  
[9] Eck, J. S., Lee, Y. K., Walker, J. C. Phys. Rev. 163 (1967), 1295.

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### МОМЕНТЫ ИНЕРЦИИ И ГИРОМАГНИТНЫЕ ОТНОШЕНИЯ НЕКОТОРЫХ ЧЕТНО-ЧЕТНЫХ ЯДЕР ИЗ РЕДКОЗЕМЕЛЬНОЙ ОБЛАСТИ.

С применением кранкинг-модели вычислены моменты инерции и гиromагнитные отношения некоторых четно-четных ядер из редкоземельной области. В расчетах применены, за исключением парных корреляций, асимптотические собственные функции модели деформированных оболочек. Сравнение с экспериментальными данными показывает хорошее согласие.