ANTIPROTON ABSORPTION CROSS-SECTION

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Parametrization of nuclear absorption cross-section of antiprotons is discussed. A simple procedure of performing the parametrization is presented and used to predict the values of the absorption cross-section.

1. INTRODUCTION

During the last fifteen years or so several experiments have reported measurements of the absorption cross-section of \bar{p} on many complex nuclei. Such measurements have been made at different values of the \bar{p} laboratory momentum. The relevant information is given in Table 1.

As seen from Table 1, the absorption cross-section has been measured over a wide range (from 368 MeV/c to 280 GeV/c) of the incident momentum of the \bar{p} , and on a large number of nuclei from He to U. Of course, gaps in the incident momentum range exist, and there are many nuclei on which measurements have not yet been made. It must also be pointed out that the information on low energy antiproton-nucleus (\bar{p} -A) interactions is meagre, though a great deal of interest in such interactions has been aroused on account of the CERN facility Low Energy Antiproton Ring (LEAR). However, sufficient data are now available on the basis of which the dependence of the \bar{p} absorption cross-section on complex nuclei can be more systematically studied, and its dependence on the \bar{p} incident momentum and the mass of the complex nucleus can be examined.

Analysis of the data should provide insight not only into the nature of the \bar{p} interaction with nuclear matter but also information useful in the determination of parameters of the \bar{p} — nucleus potential. It is for these reasons that an analysis of the entire published data (as available to us) is being attempted in this work. We believe this is the first work of this kind. In this work, only the relevant part of the published data is given. The rest of the data may be found elsewhere [1—8].

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Experimental measurements

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	(60, 200 and 280) GeV/c		(20, 30 and 40) GeV/c		(6.65, 13.3 and 25) GeV/c	GeV/c in 0.05 GeV/c steps	In the region (1.0 to 3.3)	(470 and 880) MeV/c	Six values between	(513, 633) MeV/c	(485, 597) MeV/c	$(368 \pm 43) \text{MeV/c}$	S. No. \bar{p} lab-momentum
and Pb	Li, C, Al, Cu, Sn	Cu, Sn, Pb and U	He, Li, Be, C, Al	Cu, Sn, and Pb	Li, Be, C, Al	C, C1		C, AI, Cu		Al, Cu, Pb	C, Al, Cu	C, Pb	Complex Nuclei
 [5] Carroll et al. (1979)		[4] Allaby et al. (1971)		[1] Denisov et al. (1973)		[6] Abrams et al. (1971)		[8] Nakamura et al. (1984)		[2] Ashford et al. (1985)	[3] Aihara et al. (1981)	[7] Cohn et al. (1984)	Reference

2. SUMMARY OF THE EARLIER ANALYSIS

(a) Parametrization

In earlier works [1—6] the $(\bar{p}-A)$ absorption cross-section (σ_a) has been parametrized according to the expression

$$\sigma_a = \sigma_0 A^a, \tag{1}$$

where σ_0 and α are adjustable parameters and A is the mass number of the nucleus with which \bar{p} interacts. For obtaining a better fit of the experimental data, the values of the two parameters, σ_0 and α , are adjusted by the method of least squares. It is observed that the value of the parameter α remains almost constant for all nuclei at one value of the \bar{p} incident momentum. The values of this parameter chosen previously are in the range of 0.61 to 0.713 for the \bar{p} momentum varying up to 280 GeV/c.

(i) Ambiguity

The fact that the parametrization involves two adjustable parameters leaves room for ambiguity and makes the task laborious and time-consuming. For example, the values of σ_0 and α obtained [1] from the least-squares fitting for the nuclei Li, Be, C, Al, Cu, Sn and Pb at a \bar{p} — momentum of 6.65 GeV/c are 72.6 \pm 1.7 and 0.624 \pm 0.006, respectively. However, these are average values found for the above-mentioned seven nuclei. To reproduce the experimental data (i.e., the $(\bar{p}$ -A) absorption cross-section) for any of the seven nuclei, the

average values of σ_0 and α have to be varies. This can be done by keeping fixed the value of either of the two parameters and varying the value of the other parameter, or by varying the values of both the parameters. Thus, there may be three sets of values of σ_0 and α for reproducing the experimental resuts for one nucleus and for one value of the \bar{p} momentum. This introduces ambiquity. There is no scope for getting unambiquous results.

(ii) Limited Applicability

The average values of σ_0 and α obtained for a particular set of nuclei (e.g., the set of seven nuclei mentioned above) are applicable only to this set of nuclei (i.e., only to those nuclei which are included in the X^2 -fitting) for one value of the \bar{p} momentum. In other words, the values of σ_0 and α are specific to a particular set of nuclei for which experimental values of absorption cross-sections are available for a given value of the \bar{p} momentum.

These values, therefore, cannot be used to discern any systematic, regular behaviour of the \bar{p} -nucleus absorption cross-section. Nor can these values be used to predict the values of a \bar{p} -nucleus absorption cross-section in other nuclei if these have been deduced for a group of nuclei at some particular value of the \bar{p} -momentum. Not only this, the absorption cross-section of \bar{p} in the same group of nuclei cannot be estimated at another value of the \bar{p} -momentum if it is known at one value of the \bar{p} -momentum.

iii) Reduced Utility

Thus, the procedure of parametrization outlined above (and, adopted hitherto) has only one merit. The merit is that the experimental data can be reproduced for a given set of nuclei for one value of the \bar{p} -momentum. However, the ambiguity and limited applicability, as discussed herein, reduce its utility. The procedure fails to provide any guidance as regards the behaviour of different nuclei at different values of the \bar{p} -momentum.

(b) Other techniques

Attempts have been made to reproduce the experimental results of the $(\bar{p}-A)$ absorption cross-section by making use of the optical model and Glauber's multiple scattering approaches [9]. However, ambiguity and lengthiness of the procedure involving several parameters do not permit satisfactory reproduction of the data.

. PRESENT ANALYSIS

An analysis of the entire published data (available to us) on the $(\bar{p}-A)$

absorption cross-section [1-8] is made in the present work with a view to finding whether

- (i) the procedure of fitting the data can be simplified
- (ii) the number of parameters can be reduced
- (iii) the ambiguity can be eliminated; and
- (iv) any regular features of the cross-section as a function of nuclear mass, and the momentum of the \bar{p} can be inferred.

4. PROCEDURE OF THE ANALYSIS

The fitting of the $(\bar{p}-A)$ absorption cross-section (σ_a) starts, in this work also, with the expression (1) given in sec. 2(a), viz,

$$\sigma_a = \sigma_0 A^a.$$

The results of this work indicate that the fitting reproduces experimental data to a fair extent if the parameter α is assigned a fixed value, namely, if $\alpha = 0.68$. Thus, only one parameter σ_0 is involved in the fitting procedure while the fitting done earlier [1—6] by other workers used two adjustable parameters as mentioned in section 2(a).

Although expression (1) yielded satisfactory results, two questions remained to be answered.

- 1. Is expression (1) applicable to σ_a for all nuclei and at all values of the \bar{p} -momentum and,
- 2. Is the numerical value (0.68) of the index α valid for every nucleus and for each \bar{p} -momentum?

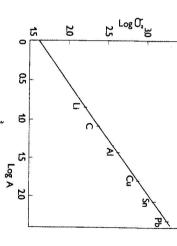
It may be mentioned that expression (1) had been applied only to a limited set of data [1, 3]. Consequently, answers to questions raised above were urgently needed.

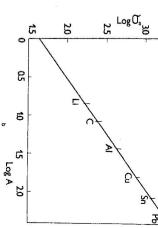
5. VARIATION OF THE PROCEDURE

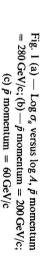
Now that a lot more data have become available, the procedure of analysis has been varied even though the starting step is still expression (1). However, now the value of the index a is not taken fixed (i.e., $a \neq 0.68$). To estimate the values of the parameters σ_0 and a the logarithm of both sides expression (1) is taken. Thus,

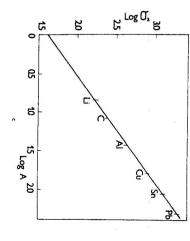
$$\log \sigma_a = \alpha \log A + \log \sigma_0 \tag{2}$$

This is the equation of a straight line. Therefore, a graph between the two known variables, $\log \sigma_a$ and $\log A$, for any value of the \bar{p} -momentum, should provide values of the two parameters; the slope of the line gives the value of the parameter a while the intercept of the line gives that of the parameter σ_0 .





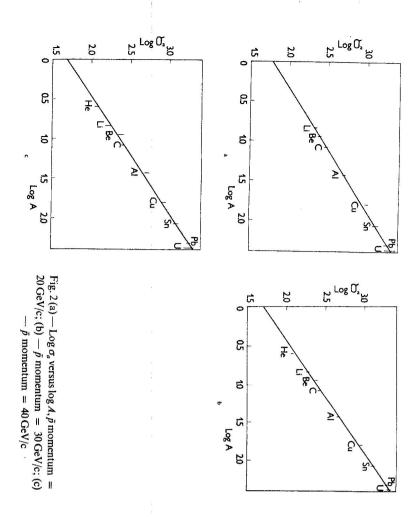




6. RESULTS AND DISCUSSION

 $\log \sigma_a$ versus $\log A$ for various values of the \bar{p} momentum are shown in Figs. 1 to 5. The slope (tan Θ) of the curves and their intercepts on the Y-axis provide values of the parameters a and σ_0 . The values of these parameters along with other relevant data are presented in Tables 2 to 6.

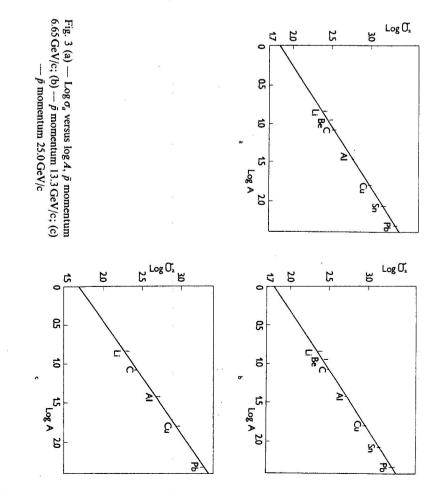
It is noteworthy that the entire experimental data, (for \bar{p} momentum from 0.485 GeV/c to 280 GeV/c) follow the pattern suggested by expression (2). A slight, irregular deviation from the general pattern (of the data falling on a straight line) is seen (Figs. 2 and 3) in the case of light nuclei He, Li and Be in the sense that the experimental data for these nuclei do not exactly fall on a straight line. This deviation (at high values of the \bar{p} momentum from 6.65 GeV/c onwards) is probably a consequence of the uncertainties of experimental data. In the absences of more and systematic deviations it would be hazardous to draw any inferences regarding any possible difference in the response of a

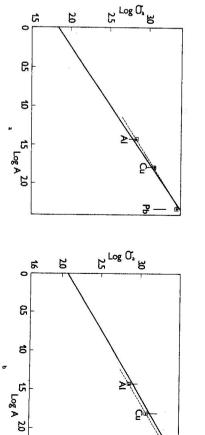


new-nucleon system and that of a many-nucleon system to the \bar{p} having the same (high) linear momentum.

Figs. 1, 2, and 3 show the behaviour of the absorption cross-section of \bar{p} having the momentum from 6.65 GeV/c to 280 GeV/c in agreement with expression (2). However, Fig. 4 tells a different tale. The experimental data of Ashford et al. [2], used in Fig. 4, do not fall on a straight line. At the same time, the calculated values of σ_a (obtained from an optical model fit) of these authors do fall on a straight line. Naturally, for purposes of this work, so far as drawing general inferences is concerned, the calculated values of Ashford et al. [2] are taken into consideration. It is worth mentioning that the calculated value of σ_a of Ashford et al. [2] for the \bar{p} absorption in Pb is in agreement with the corresponding value estimated in the present work. The \bar{p} momentum varies from 0.514 GeV/c to 0.633 GeV/c at which Ashford et al. have reported their results.

Fig. 5 shows that σ_a for the \bar{p} momentum from 0.485 GeV/c to 0.597 GeV/c follows the expected behaviour, i.e., the data points fall on a straight line.





 $0.368 \, \text{GeV/c}$ (i.e., by $0.146 \, \text{GeV/c}$) in the \bar{p} momentum results in an increase in

(730 \pm 180) mb in the case of C. Similarly, a decrease from 0.514 GeV/c to

by 0.117 GeV/c) the cross-section σ_a increases from (410 \pm 35) mb to

the value of σ_a from (2100 \pm 700) mb to (5300 \pm 1700) mb in the case of Pb. It

 \bar{p} momentum of 0.514 GeV/c, σ_a for Pb is (2100 \pm 700) mb (Table 5). These

value of (0.485 + 0.036) GeV/c, σ_a is (410 ± 35) mb for C (Table 6) while at the

values show that as the \bar{p} momentum decreases from 0.485 GeV/c to 0.368 GeV/c

 \bar{p} momentum of 280 GeV/c, respectively. Even at the \bar{p} momentum of the low C and Pb go on decreasing, becoming (239 \pm 8) mb and (1856 \pm 77) mb at the

 (5300 ± 1700) mb for Pb while (as seen from Tables 2 to 6) the values of σ_a for value at which experimental data are available), is (730 \pm 180) mb for C and

from Table 8, the value of σ_a at the \bar{p} momentum of 0.368 GeV/c (the lowest numerous to permit generalization. It is also worth mentioning that, as seen (b) The experimental values of σ_a for low values of the \bar{p} momenta are not 0.514 GeV/c and 0.633 GeV/c do not fall, as already mentioned, on a straight

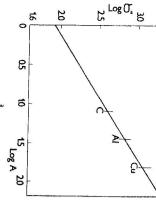
(a) The experimental values of σ_a of Ashford et al. [2] for the \bar{p} momenta of

line and obviously do not obey expression

What does this disagreement mean?

with caution for several reasons:

given value of the \bar{p} momentum. However, the temptation should be tempered \bar{p} absorption cross-section, if not for all \bar{p} momenta, at least for all nuclei at a available) and that the Figs. 1 to 5 could be used for predicting the values of the



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Fig. 5 (a) — $\log \sigma_a$ versus $\log A$, \bar{p} momentum 0.485 GeV/c; (b) — \bar{p} momentum 0.597 GeV/c

In can, thus, be inferred that the entire available experimental data, for al

expression (2). In the light of this inference it is tempting to generalize and say

made and whose results have been reported) follow the pattern suggested by values of the $ar{p}$ momentum and for all nuclei (for which experiments have been

that expression (2) is or should be valid for all \bar{p} momenta and for all nuclei (i.e.,

for those \bar{p} momenta and nuclei for which experimental data are not

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. Table 2 \bar{p} absorption cross-section and values of parameters σ_0 and α \bar{p} momentum 60 GeV/c,

	<u></u>				oo Gev/c and	200 GeV/C				
\bar{p} momentum		Nuclea	ır absorptio	on cross-sec	ction, σ_a (mb))	Results of Ca	rroll et al [5]	Results of	this work
(GeV/c)	Li	С	Al	Cu	Sn	Pb	σ_0	α	σ_0	α
60 200 280	163 ± 5	236 ± 7		772 ± 24	1218 ± 38 1239 ± 40 1236 ± 51	1805 ± 56 1793 ± 58 1856 ± 77	43.50 ± 1.73 41.08 ± 1.67 41.05 ± 1.91	0.698 ± 0.010 0.710 ± 0.011 0.713 ± 0.013	43.65 41.69 40.74	0.696 0.704 0.713

Table 3 \bar{p} absorption cross-section and values of parameters σ_0 and α p momentum 20 GeV/c, 30 GeV/c, and 40 GeV

p̄ mo- mentum				Nuclear a	bsorption	cross-section	n, σ_a (mb)			1	of Allaby al. [4]	Resul this v	
(GeV/c)	He	Li	Be	С	Al	Cu	Sn	Pb	U	σ ₀ (mb)	α	$\sigma_0(mb)$	α
20 30 40	117 ± 5	188 ± 4	235 ± 6	258 ± 6	457 ± 11	890 ± 30	1210 ± 45	1880 ± 65	2020 + 125	50.9 + 2.4	0.648 ± 0.010 0.674 ± 0.009 0.674 ± 0.010	50.12	0.63 0.67 0.67

Table 4 \bar{p} absorption cross-section and values of parameters σ_0 and α \bar{p} momentum 6.65 GeV/c, 13.3 GeV/c and 25.0 GeV/c

\bar{p} momentum		Nu	clear absor	rption cros	s-section,	σ_a (mb)			of Denisov al. [1]	Resul this v	
(GeV/c)	Li	Be	С	Al	Cu	Sn	Pb	σ ₀ (mb)	α	σ_0 (mb)	α
6.65	252 ± 6	296 ± 6	330 ± 7	558 ± 10	952 ± 20	1421 ± 53	2056 ± 42	72.6 ± 1.7	0.624 ± 0.006	69.18	0.634
13.3								67.0 ± 1.2	0.636 ± 0.005	63.10	0.648
25.0	200 ± 5		265 ± 6	480 ± 9	862 ± 20	_	1849 ± 45	58.7 ± 1.4	0.629 ± 0.007	48.98	0.683

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 \bar{p} absorption cross-section and values of parameters σ_0 and a \bar{p} momentum 0.514 GeV/c and 0.633 GeV/c

0.633		$ ilde{p}$ momentum
620 ± 500	AI AI	Nuclear ab
1100 ± 100	Cu	Nuclear absorption cross-section, σ_a (mb)
1400 ± 700 1400 ± 250	Pb	
91.2	σ ₀ (mb)	Results of Ashfordet al. [2]
0.61	a	Ashford [2]
67.61	σ ₀ (mb)	Results of this work
0.669	a	of this

lable b

 \bar{p} absorption cross-section and values of parameters σ_0 and a \bar{p} momentum 0.485 \pm 0.036 GeV/c and 0.597 \pm 0.024 GeV/c

0.485 ± 0.036 410 ± 35 663 ± 86 0.597 ± 0.024 422 ± 25 679 ± 66	(GeV/c)	$ar{p}$ momentum
410 ± 35 422 ± 25	С	Nuclear al
663 ± 86 679 ± 66	Αl	sorption σ_a (mb)
1186 ± 154 1188 ± 106	Cu	Nuclear absorption cross-section, σ_a (mb)
87.9 ± 16.3	တ္မ (mb)	Results of Ai et al. [3]
0.62 ± 0.06	a	Results of Aihara et al. [3]
83.18 89.13	σ ₀ (mb)	Results of this work
0.634 0.620	a	ts of ork

Table 7

 \bar{p} absorption cross-section and values of parameters σ_0 and α \bar{p} momentum 0.628 GeV/c, 0.782 GeV/c and 0.881 GeV/c

0.626 0.782 0.881	(004/0)	p̄ momentum	
727 ± 30 720 ± 30 661 ± 30	lV	Nuclear absorption cross-section σ_a (mb)	
1197 ± 40 1198 ± 40 1118 ± 40	Cu	on cross-section, mb)	
Not estimated	σ_0 (mb) a	Results of Nakamura et al. [8]	
104.7 104.7 87.0	σ ₀ (mb)	Results of this work	
0.588 0.586 0.616	a	of this	

Table 8

 \bar{p} absorption cross-section and values of parameters σ_0 and α \bar{p} momentum 0.368 GeV/c

0.368	(004/0)	p̄ momentum
730 ± 180	С	Nuclear absorption σ_a (
5300 ± 1700	Pb	Nuclear absorption cross-section, σ_a (mb)
Not estimated	σ_0 (mb) α	Results of Cohn et al. [7]
130.3	σ ₀ (mb)	Results of this work
0.695	a	of this

lable

 \bar{p} absorption cross-section and the values of parameters σ_0 and a \bar{p} momentum 1.6 GeV/c to 3.2 GeV/c in steps of 0.2 GeV/c

\bar{p} momentum	Nuclear absorption cross-section σ_a (mb)	on cross-section, mb)	* Results	* Results of Abrams et al. [8]	Results of this work	of this
(05/6)	С	Cu	σ_0 (mb)	a	σ ₀ (mb)	a
1.6	396.33 ± 1.20	1131.01 ± 6.35			85.11	0.621
1.8	391.53 ± 1.20	1099.24 ± 6.35			83.18	0.623
2.0	385.52 ± 1.20	1080.18 ± 6.35			86.10	0.608
2.2	379.52 ± 1.20	1080.18 ± 6.35			79.43	0.628
2.4	373.51 ± 1.20	1067.47 ± 6.35			74.13	0.642
2.6	366.31 ± 1.20	1048.41 ± 6.35			72.44	0.644
2.8	360.30 ± 1.20	1042.06 ± 6.35			72.44	0.644
3.0	349.49 ± 1.20	1029.35 ± 6.35			68.39	0.653
3.2	341.08 ± 1.20	1010.29 ± 6.35	68 ± 7	$68 \pm 7 0.65 \pm 0.01$	66.07	0.656

^{*}Abrams et al obtained the average values of σ_0 and α at 3.2 GeV/c

is obvious, therefore, that more experimental values of σ_a at lower values of the \bar{p} momentum would be needed to draw any meaningful inferences. It is also noteworthy that at a low \bar{p} momentum (0.368 GeV/c) the error in the value of σ_a is about 25% for the C nucleus and about 32% for the Pb nucleus. Thus, it cannot be said without any measure of certainty that expression (2) is, or would be, equally valid at lower values of the \bar{p} momenta.

(C) The third cause for caution lies in the likely response of very light nuclei like He, Li and Be to the \bar{p} momenta of different, particularly lower values. Will the response be the same as that of heavier nuclei?

The only safe statement that can be made is that expression (2) seems to be generally valid over the \bar{p} momentum range from (0.485 \pm 0.036) GeV/c to 280 GeV/c, and that over this range the value of σ_a can be predicted, for a given value of the \bar{p} momentum, for complex nuclei for which experimental results are not available. Figs 1 to 5 become, therefore, very important. The value of σ_a for any complex nucleus can be obtained from them.

In certain cases [6—8], experimental values of σ_a for a given \bar{p} -momentum are available only for two nuclei as seen from Tables 7 to 9. It is obvious that no curve can be plotted on the basis of two points. However, assuming that the aforementioned inference regarding the validity of expression (2) is correct, we have hazarded a guess about the values of the parameters α and σ_0 which are presented in the last columns of tables 7 to 9.

The values of the parameters α and σ_0 estimated in this work (from Figs. 1, 2, 3 and 5) compare with the values of these parameters as obtained by other

obtained from the datum are expected to have different values. into account. If the datum behaves differently, the values of the parameters columns of Tables 2, 3, 4 and 6. However, the values obtained from Ash. that experimental datum of these authors does not obey expression (2) is taken ing values of this work (Table 5). This difference falls in perspective if the fact workers from a chi-square fit. The two sets of values are given in the last ford et al..[2] of these parameters considerably differ from the correspond-

nuclei in which the \bar{p} absorption has not been studied so far. reproduce experimental data but also to predict the value of σ_a even in those parametrization suggested in this work is reliable and can be used not only to adjusting the value of the other parameter. Therefore, it seems to us that the possible to change the value of one parameter and compensate the change by parametrization of the nuclear absorption cross-section of \bar{p} . It is no more automatically takes care of the ambiguity encountered in other methods of The unique set of the values of the parameters α and σ_0 obtained in this work

7. CONCLUSIONS

- results is possible. (i) A simple method of parametrization of σ_a which yields unambiguous
- experimentally studied can be predicted for a given value of the \tilde{p} momentum. (ii) The value of σ_a for nuclei in which the \bar{p} absorption has not been
- available. 450 MeV/c) can be tested only when more relevant experimental data become as, and more particularly, for low values of the \bar{p} momentum (say below (iii) The validity of the analysis of this work in the case of light nuclei as well

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ДИФФЕРЕНЦИАЛЬНОЕ СЕЧЕНИЕ АНТИПРОТОННОГО ПОГЛОЩЕНИЯ

для предсказания значений дифференциаяльного сечения подлощения. протонов. Описана простая процедура проведения параметризации, которая использована Обсуждается параметризация дифференциального сечения ядерного поглощения анти-