DIFFUSION OF ZINC IN DOPED NaCI CRYSTALS

VIERA PAULÍNY-TÓTHOVÁ, Bratislava

INTRODUCTION

The bivalent cationic (hereafter b. c.) admixtures move through the lattice of alkali halides by changing places with the neighbouring vacancy, so their diffusion is possible only when they form neutral complexes: admixture—cation vacancy. The complexes are formed as a result of electrostatic interaction between excess positive charge of admixture and virtual negative charge of the cation vacancy. Lidiard [1] examined theoretically the dependence of the diffusion coefficient of b. c. admixtures in alkali halides on their degree of association, i. e. on the ratio of the complex number to the total number of ions of the given admixture. When the admixture forms a very diluted solid solution then in a simple model the association—dissociation reaction determining the number of complexes obeys the law of mass action

(free admixture concentration). (free cation vacancy concentration) = K

where K(T) is the reaction constant depending on absolute temperature, on the number of possible complex orientations and on the association energy of these complexes. It follows from Eq. (1) that the association degree of the admixture in "pure" crystals depends on its concentration, hence its diffusion coefficient will also depend on the concentration.

The b. c. admixtures are built substitutionally into the lattice of most of the alkali halides. In order to preserve the charge neutrality the same number of cation vacancies is formed simultaneously. If the b. c. admixture Zn diffuses into the crystal containing another b. c. admixture M in a substantially higher concentration, the number of free vacancies will practically be determined by the concentration and association energy of admixture M. This number will be high in comparison with a "pure" crystal and it will not depend on the concentration of admixture Zn. The association — dissociation reaction will be displaced toward the higher complex concentration and the association

degree of the admixture Zn will practically not be dependent on its proper concentration. The diffusion coefficient of the admixture Zn will not depend on Zn-concentration and it will grow with increasing M-concentration.

The aim of this paper was:

- 1) to prove the concentration independence of the diffusion coefficient of zinc (hereafter D) in doped NaCl crystals,
- 2) to compare the effects of different b. c. admixtures on D,
- 3) to analyze diffusion without vacancy gradient,
- 4) to obtain information about D at higher association degrees of Zn. An estimation of the association energy of added admixtures and of zinc should be possible by comparison of the shape of diffusion isotherms (D versus admixture concentration at the constant temperature T).

The formation of bigger agglomerates of admixtures with vacancies [2] and the formation of vacancy pairs the concentration of which is negligible [3], was not taken into account here.

Theoretical

a) Diffusion in "pure" crystals

According to Lidiard [1] at high concentrations c_{Zn} of the diffusing ions, when $4K_{Zn}c_{Zn} \gg 1$ (1) and, therefore, the degree of association is high, D reaches its saturated value D_0 . At lower concentrations D decreases with the decreasing concentration of the diffusing ions. When $c_{Zn} \ll c_M$, where c_M is the total concentration of b. c. impurities in the crystal, it may be expected, that D will be independent on the concentration c_{Zn} (see b) below). In this case Eq. (1) may be written

(2)
$$\frac{p_{\rm Zn}}{(1 - p_{\rm Zn})(1 - p_{\rm M})c_{\rm M}} = K_{\rm Zn},$$

where p_{Zn} and p_M are the association degrees of the diffusing ions (zinc) and of b. c. impurities (predominantly Ca), respectively. When $p_M \ll 1$ and $K_{Zn}c_M \ll 1$ which may be expected at small c_M and at higher temperatures, then

$$p_{\rm Zn} = K_{\rm Zn} c_{\rm M}$$

and

$$D
ightharpoonup D_0 \ K_{
m Zn} \ c_{
m M}$$

(4)

 $^{^{(1)}}K_{\mathrm{Zn}}$ is the reaction constant of the Eq. (1) for complexes of the diffusing ions.

since, according to Lidiard [1],

$$D=D_0rac{d(p_{
m Zn}\,c_{
m Zn})}{dc_{
m Zn}}$$
 .

than those previously published [4, 5]. of the b. c. impurities present. The values of D should be substantially lower enables to lower c_{Zn} , it may be expected from Eq. (4) that the D obtained will be independent on c_{2n} and approximately proportional to the concentration If the diffusion is traced by means of an isotope with high specific activity which

b) Diffusion in NaCl + MCl₂ crystals

tively, free cation and anion vacancies with molar concentrations $x_{
m pos}$, $x_{
m neg}$, respecdescribed by the following equations: a) for the dissociation of the lattice on In a doped crystal the formation of free vacancies and complexes may be

(5)
$$x_{\text{pos}} \cdot x_{\text{neg}} = K_0^{-1};$$

b) for complex formation of the diffusing b. c. ions

(6)
$$\frac{p_{\rm Zn}c_{\rm Zn}}{(1-p_{\rm Zn})c_{\rm Zn}x_{\rm pos}} = K_{\rm Zn};$$

c) for complex formation of the uniformly built-in admixture M₊₊

$$\frac{p_{\text{M}} c_{\text{M}}}{(1 - p_{\text{M}}) c_{\text{M}} x_{\text{pos}}} = K_{\text{M}}$$

 K_0^{-1} , $K_{\rm Zn}$, $K_{\rm M}$ are the respective reaction constants depending only on temperature;

d) the charge neutrality condition must be fulfilled

$$x_{\text{pos}} = x_{\text{neg}} + (1 - p_{\text{Zn}})c_{\text{Zn}} + (1 - p_{\text{M}})c_{\text{M}}$$

which can then be written more simply in doped crystals $x_{\rm neg} \ll 5$. 10⁻⁶ mol. fr.; $x_{\rm neg}$ may be neglected in Eq. (8) free vacancies. From Eq. (5) and from published data [7] it can be shown that According to literature [6, 7] pure NaCl at 590 °C contains (5-7). 10-6 mol fr.

$$x_{pos} = (1 - p_{Zn})c_{Zn} + (1 - p_{M})c_{M}$$

Eqs. (6), (7), (8) lead to one cubic equation for $p_{Zn}(c_{Zn}, c_M, K_{Zn}, K_M)$.

 p_{Zn} and x_{pos} should be independent of c_{Zn} . The Eq. (6) will be more simple $c_{
m M}\!\gg\! c_{
m Zn}$, D does not depend on $c_{
m Zn}$. According to [1] and Eq. (6) in this case The measured diffusion profiles (Fig. 2) show that in doped crystals, when

$$(10) x_{\text{pos}} \doteq (1 - p_{\text{M}})c_{\text{M}}.$$

In this case it is suficient to solve two equations

(11)
$$\frac{p_{Z_n}}{1 - p_{Z_n}} = K_{Z_n} c_M (1 - p_M),$$

(12)
$$\frac{p_{\rm M}}{1 - p_{\rm M}} = K_{\rm M} c_{\rm M}$$

Solving Eqs. (11), (12) we get

(13)
$$p_{\rm Zn} = \frac{K_{\rm Zn}}{2K_{\rm M}} \cdot \frac{\sqrt{1 + 4K_{\rm M}c_{\rm M}} - 1}{1 + \frac{K_{\rm Zn}}{2K_{\rm M}} [\sqrt{1 + 4K_{\rm M}c_{\rm M}} - 1]}$$
and for D

and for D

(14)
$$D = D_0 \left\{ 1 - \frac{1}{1 + \frac{K_{\rm Zn}}{2K_{\rm M}}} \left[\sqrt{1 + 4K_{\rm M}c_{\rm M}} - 1 \right] \right\}$$
 From Eq. (14) it may be seen that D will be little dependent

equal, D will slightly decrease. creasing association energy of different admixtures their concentration being the association energy of the admixture added and $\lim_{\alpha_{M}\to\infty} D = D_0$. With in-From Eq. (14) it may be seen that D will be little dependent on $K_{\mathbb{M}}$ i. e. on

Experimental

of diffusion annealing and then rapidly cooled. After this treatment the samples cleft off the latter were heated before diffusion for six hours at the temperature were practically clear. Crystals with CdCl₂ content higher than 0,03 mol—% were ,,milky". Samples by Dreyfus [8]. The total concentration of b. c. impurities is in the range ture concentration in the melt and in the crystal differs from the ratio given and of naturally present impurities by spectral analysis. The ratio of admixand Zn contents in crystals were determined by colorimetry, the content of Ca method. The b. c. admixtures were added to the melt as chlorides. The Cd (1-3). 10-6 mol. fr., the alcalinity of samples is lower than 10-4 mol. fr. The NaCl crystals used were grown in nitrogen surroundings by Kyropoulos'

so that their active surfaces were adjacent and heated at 590 °C in an N₂ were cleft off. atmosphere. After diffusion annealing 3 mm from the sides of the samples to one surface of samples measuring $14 \times 14 \times 5$ mm. Two samples were coupled The ZnCl₂ layer (labelled by Zn⁶⁵) approximately 2μ thick was evaporated on

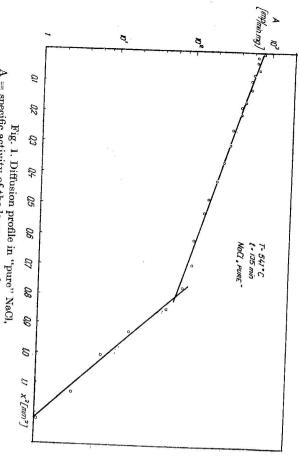
a single channel amplitude analyzer Tesla was used method previously described [4]. For the activity measurement of slices naturally present is considerable. The diffusion profile was determined by the be limited by low Cd solubility. At low Cd concentrations the effect of calcium The annealing temperature was chosen sufficiently high in order not to

Results

equation holds good: layer into a semi-infinite body. In this case, if D is constant, the following By our experiments we nearly approached diffusion from an infinitely thin

(A)
$$c(x, t) = \frac{Q}{\sqrt{(\pi D t)}} \exp\left(-\frac{x^2}{4Dt}\right)$$

to the surface may be expected. In greater depth, if D remains constant, the rapidity, a deviation of the profile measured from Eq. (A) in the layer adjacent after t-hours' annealing. Q is the surface density of Zn in the original active linear relationship between ln c and x^2 must be satisfied. layer. As the evaporated layer does not dissolve in the crystal with infinite c(x, t) being the Zn concentration in the depth x below the original surface



A= specific activity of the layer removed proportional to c_{Zn} x =distance of layer from original surface

to the lower D (Fig. 1) in all profiles, when Zn concentration dropped to the centration in the knee was found. by the Ca⁺⁺ concentration [5]. No temperature dependence of the zinc conlevel of naturally present b. c. impurities, which is practically determined In the case of diffusion into "pure" crystals we observed an evident "knee"

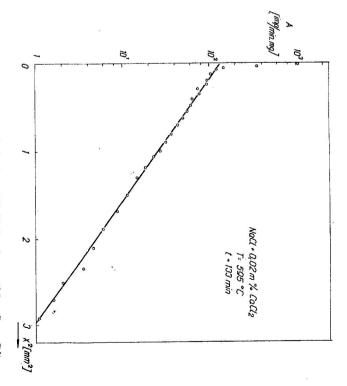


Fig. 2. Diffusion profile in doped NaCl if $c_M \gg c_{\rm Zn} \, (M={
m Ca~or~Cd})$

centration if the samples were pre-heated (see Experimental). in concentration not higher than 5 . 10⁻² mol-%, 3) cadmium in higher conserved when the following admixtures were chosen 1) calcium, 2) cadmium the whole measured Zn concentration range (Fig. 2). The linearity was prehigher than the Zn concentration, the dependence of $\ln c$ on x^2 was linear in In doped crystals where admixture concentration was by several orders

gradient. The Zn solubility in NaCl at 590 °C is only $2.5 \cdot 10^{-4}$ mol. fr. [9] of Zn as admixture and thus in achieving a diffusion without a concentration and when grown from the melt the Zn content in crystals was even much lower. We did not succeed in obtaining a linear dependance of $\ln c$ vs x^2 by means

concentration (Fig. 4), therefore, only results obtained on pre-heated samples compound diffusion profiles (Fig. 3). In the resulting dependence of D on Cd

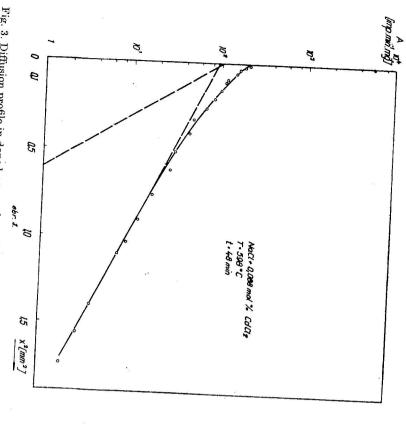


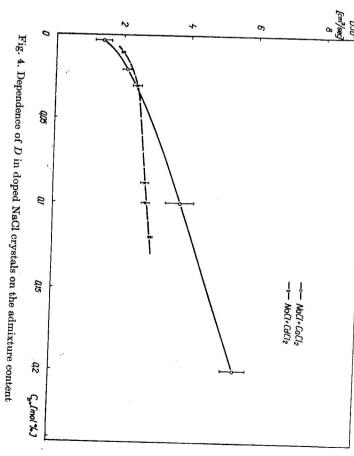
Fig. 3. Diffusion profile in doped nonpre-heated NaCl with high Cd content

Discussion

a) Diffusion in the "pure" crystal

of the shape of the diffusion profile: be at least 0,55 eV. The following facts, however, are against this explanation tion shows that the necessary association energy of $Z_{n^{++}}$ complexes should tively explained by D having reached the saturated value D_0 . A rough estimamol. fr. $\mathrm{Zn^{++}}$ (Fig. 1) follows from the linearity of $\ln c$ vs x^2 . It may be tenta-The concentration independence of D observed in the range (5-20). 10^{-5}

0,38 eV is expected, 1) according to Bassani and Fumi [10] an association energy lower than



2) our further research (see Discussion b)) shows that D_0 is substantially

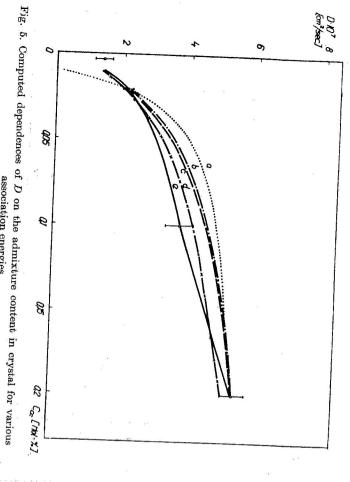
3) the concentration of the "knee" is independent of temperature.

by a modified experimental method. We are proceeding, therefore, in the investigation of diffusion in crystals

b) Diffusion of Zn in NaCl + CaCl₂ crystals

estimation of the correction caused by this interaction given by Ikeda [13] for NaCl + CdCl₂ would support this explanation. An increase of D_0 with the the interaction between free defects cannot be neglected any more. The rough effective association energy of Zn with growing admixture concentration when of D_0 at higher concentrations of admixtures. It is probable that the difference between the measured and computed shape is caused by a lowering of the curve expressing Eq. (14) is d. But the points measured are better expressed by curve e, which demands a lowering of Zn association energy and an increase K_{Ca} given in literature (Table 2). Within the limits of errors the most suitable for experimental points in the range $(2-20) \cdot 10^{-4}$ mol. fr. Ca, for various Fig. 5 shows the dependence of D on c_{c_3} computed according to Eq. (14)

372



association energies.

Ca concentration may be explained as a result of the growing defectivity of

c) Diffusion of Zn in NaCl + CdCl₂ crystals

of the Cd concentration increases neither the number of free vacancies nor the form of neutral agglomerates of cadmium ions and vacancies. mol. fr. is probably caused by the limited Cd++ solubility. A further growth D. Excess cadmium is precipitated in the form of a second phase or in the The slight dependence of D on the concentration of Cd higher than $3 \cdot 10^{-4}$

close to solubility at room temperature. The rapidly diffusing component (Fig. 3) corresponds probably to the diffusion along the boundaries of the built in the lattice in the course of diffusion annealing probably remains low ---In nonpre-heated crystals with a high Cd content the concentration of Cd

Conclusion

admixture, the D is independent of the concentration c_{Z^n} . If the diffusion of the built-in b. c. admixture is substantially higher than that of the diffusing It has been shown that in doped NaCl crystals when the concentration of

Table 1. Diffusion coefficients D and average concentrations of diffusing zinc \bar{c}_{za} in various doped NaCl crystals

		Admixture	Admirtuna		
Sample	Admixture	content in melt [mol—%]	content in crystal [mol—%]	$D.~10^7$ [cm ² /s]	$\bar{c}_{\rm Zn} \cdot 10^3 \ [{ m mol\%}]$
C 12	"pure"	1	0,003(3)	1,62	11
C 39	Zn	2		1,12	16
9	7U	0,4	5.10-4	1,55	12
C 43)) }		1,55	10
7	Ca	0,02	0,02	2,24	ယ
Э Я	2			1,98	ယ
9	Ca	0,1	0,1	4,18	4
C 44	2			3,34	2
	Ca	0,2	0,2	5,81	_
98.0	5	· •		5,07	_
0	Ğ	0,06	0,01	2,00	9
C 62	2))		1,94	9
(t		0,3	0,03	2,44	Ot.
C 81	2))	7.00	2,42	4
(Ca	0,8	0,088	2,84	O1
C 94	5) -		2,60	00
9	ç	0,8	0,12	2,95	7
				2,87	7
	2	>		2,81	œ
C 65		, <u>8</u>			
C 65		•	0,1	2,86	6

⁽³⁾ The total concentration of b. c. impurities

Table 2. Computed association energies of zinc complexes $\Delta G_{\rm Zn}$ (for different values of Ca⁺⁺-association energy $\Delta G_{\rm Ca}$ obtained from literature) for curves in Fig. 5

0,08 0,38 0,24 0,5 0,38	AG_{Ca} [eV]
[10] [12] [11]	References
$\begin{array}{c} 0,42 \\ 0,38 \\ 0,39 \\ 0,25 \text{ for } c_{\text{ca}} > 0,1 \text{ mol}\% \\ 0,42 \text{ for } c_{\text{ca}} < 0,1 \text{ mol}\% \end{array}$	$\Delta G_{ m Zn}$ [eV]
ဇည္ တာဂ ဆု	Curve in Fig. 5

the D depends both on the concentration of the diffusing substance and on and so to achieve a diffusion without vacancy gradient. In "pure" crystals tion gradient cannot be performed, it is more convenient to use doped crystals a poorly soluble substance is investigated, where a diffusion without concentratration of the admixture which is known. the purity of the crystal. In doped crystals the D depends only on the concen-

Cd complexes. only for small concentrations of Ca and Cd (Fig. 4). It suggested that the association energy of Ca complexes is the same or a little higher than that of The comparison of the diffusion isotherms for NaCl + CaCl₂ was possible

shows that the effective association energy of Zn complexes will decrease with increasing admixture concentration. The analysis of the shape of the diffusion isotherm in Ca doped crystals

of the experimental work and to Ing. Estera Rubínová for the preparation The author is indebted to DrSc. Arnošt Kessler for his helpful discussions

REFERENCES

- [1] Lidiard A. B., Handbuch der Physik, Bd. 20, Springer-Verlag 1957.
- [2] Haven Y., Report of the Conference on Defects in Crystaline Solids, Bristol 1954.
- [3] Mapother D., Crooks H. N., Maurer R., J. Chem. Phys. 18 (1950), 1231.
- [4] Kessler A., Mariani E., Paulíny-Tóthová V., Czech. J. Phys. B 14 (1964), 34. [5] Chemla M., These, Paris 1954.
- [6] Etzel H. W., Maurer R., J. Chem. Phys. 18 (1950), 1003
- [7] Lidiard A. B., Phys. Rev. 94 (1954), 29.
- [8] Dreyfus R. W., Phys. Rev. 121 (1961), 1675.
- [9] Paulíny-Tóthová V., Popeliš I., Czech. J. Phys. B *15* (1965), 921
- [10] Bassani F., Fumi F. G., Nouvo Cim. 11 (1954), 274.
- [11] Bean C., Thesis, University of Illinois, 1952.
- [13] Ikeda T., J. Phys. Soc. Japan 19 (1964), 858. [12] Мурин А. Н., Банасевич С. М., Грушко Я. С., Физ. тверд. тела 3 (1961), 2427.

Received August 16, 1965

Slovenskej akadémie vied ČSAV, Fyzikálny ústav Bratislava